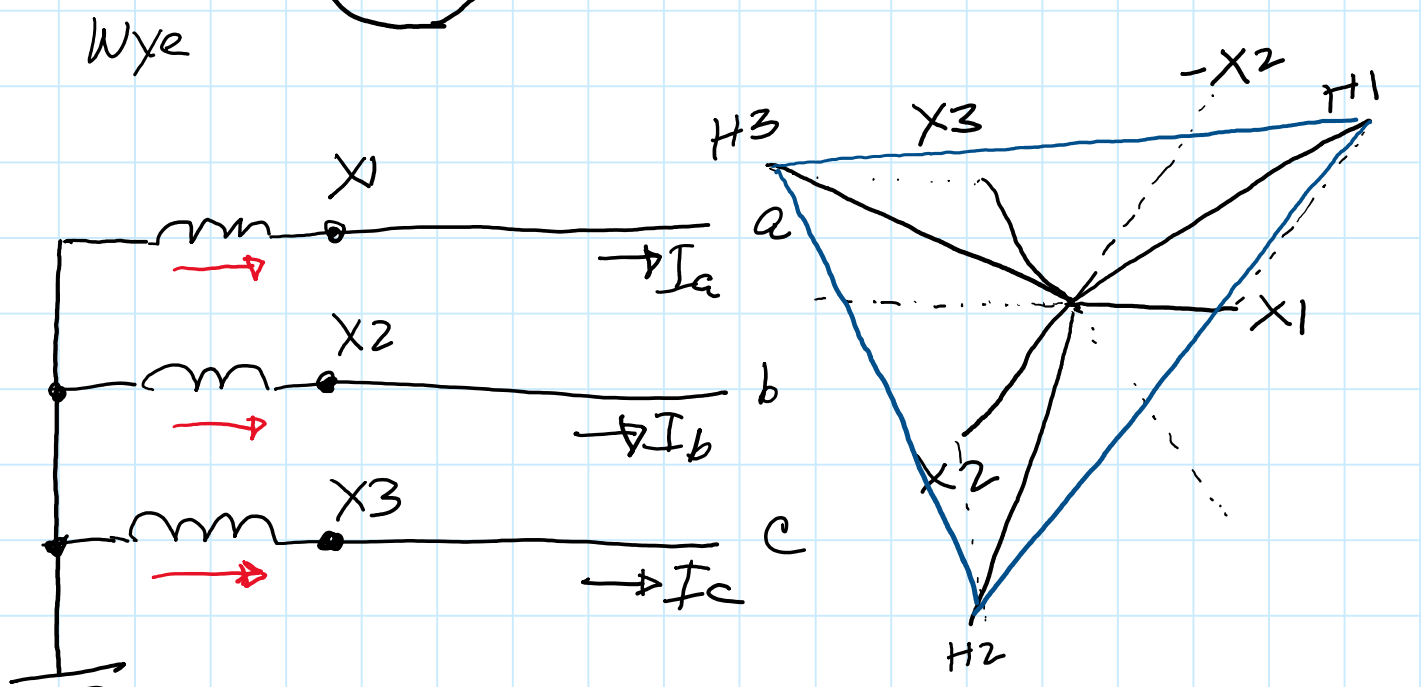
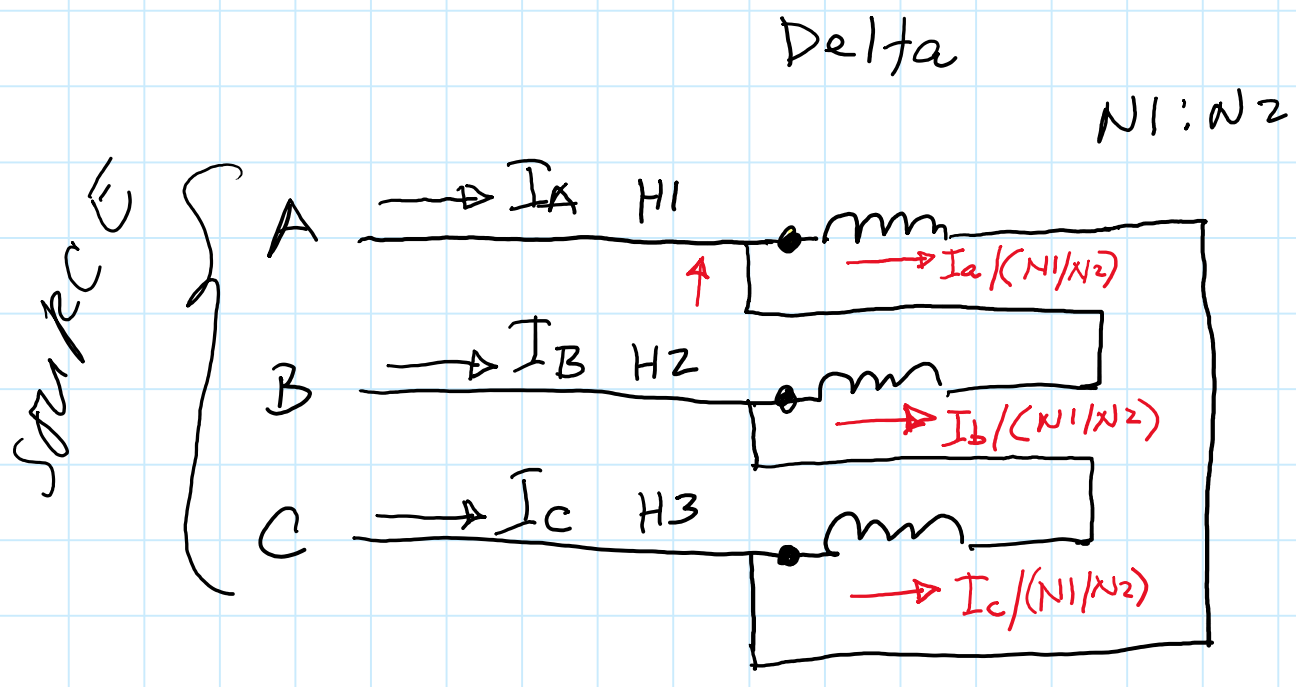
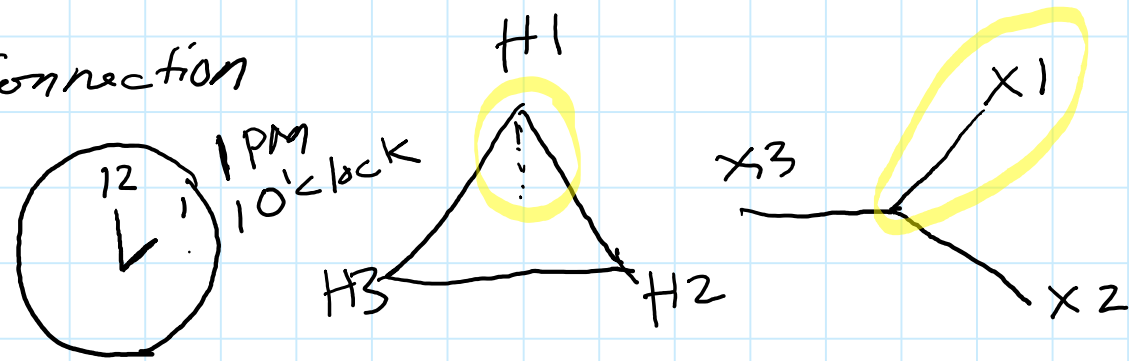
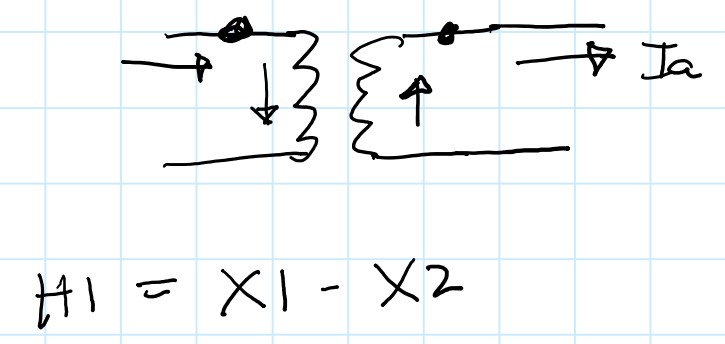
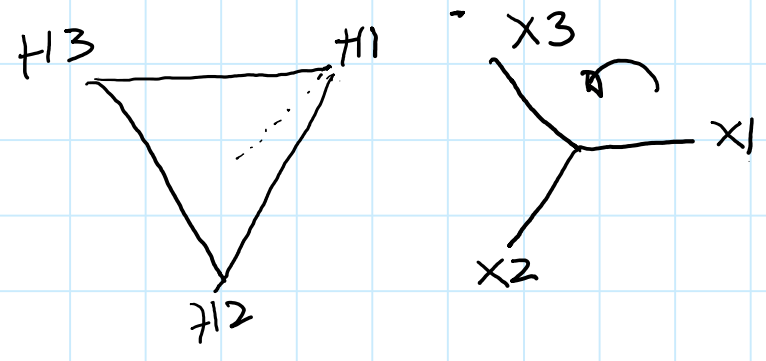


# ANSI/IEEE DABY/DY1 (IEC) Transformer Connection



Per IEEE Standard  
HV must lead LV  
by  $30^\circ$



Assuming we want to connect winding A @ HV with winding C @ LV, then at node H1:

$$I_A + I_c / (N1/N2) = I_a / (N1/N2) \rightarrow I_A = I_a / (N1/N2) - I_c / (N1/N2)$$

$$I_c = I_a \times 1 \angle 120^\circ$$

$$I_A = |I_a| \angle 0^\circ - |I_a| \angle (0^\circ + 120^\circ) = \sqrt{3} |I_a| \angle -30^\circ$$

Conclusion:  $I_A$  lags  $I_a$  by  $30^\circ$  (Does not comply with IEEE)

Assuming we want to connect winding A @ HV with winding B @ LV, then at node H1:

$$I_A + I_b / (N1/N2) = I_a / (N1/N2) \rightarrow I_A = I_a / (N1/N2) - I_b / (N1/N2)$$

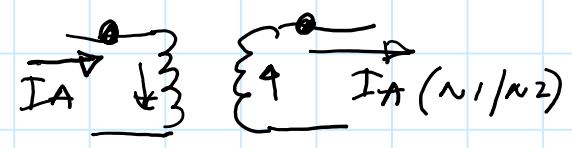
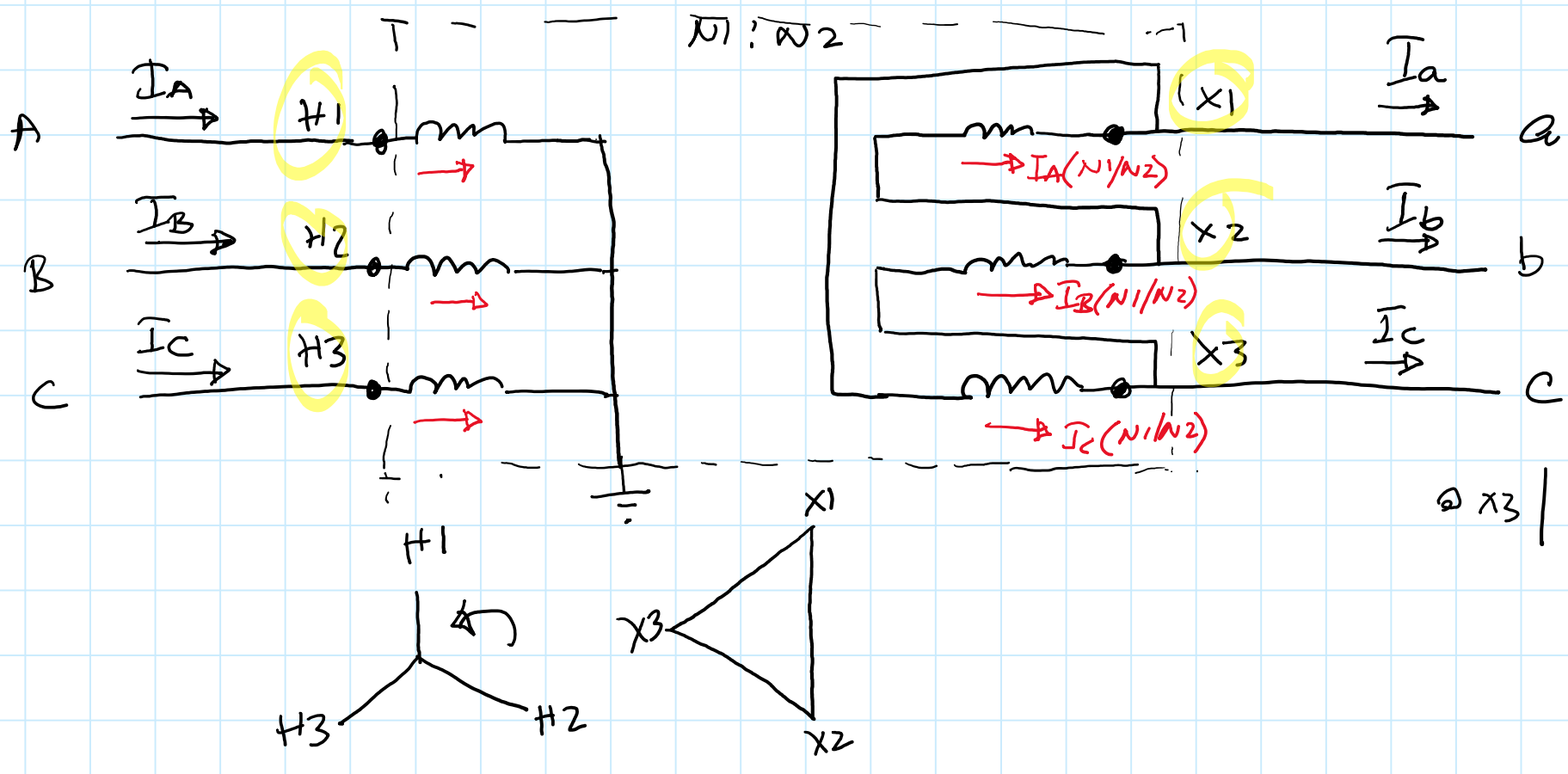
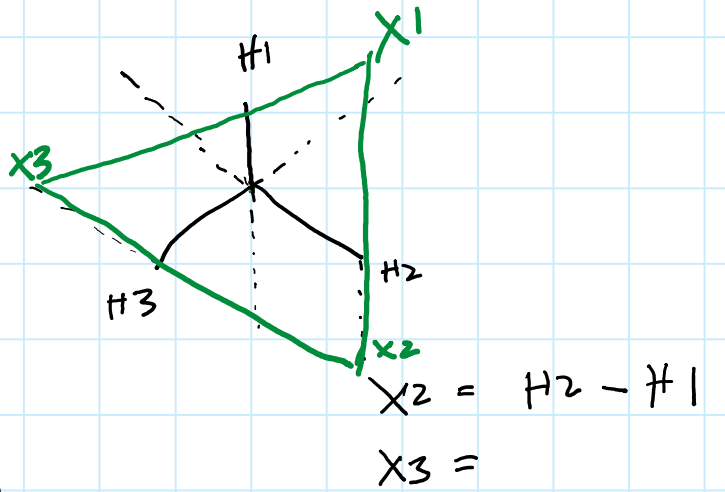
$$I_b = I_a \times 1 \angle 240^\circ$$

$$I_A = |I_a| \angle 0^\circ - |I_a| \angle (0^\circ + 240^\circ) = \sqrt{3} |I_a| \angle 30^\circ$$

Conclusion:  $I_A$  leads  $I_a$  by  $30^\circ$  (Comply with IEEE)

# ANSI YDAC / Δd Transformer Connection

$$\begin{aligned} I_B &= I_A + I_b \\ I_b &= I_B - I_A \\ X_2 &= H_2 - H_1 \end{aligned}$$



$$\begin{aligned} @ X_3 \quad I_C &= I_c + I_B \\ I_c &= I_C - I_B \\ X_3 &= H_3 - H_2 \end{aligned}$$

Assuming we connect winding "a" of LV with winding "b" of HV, then at node X1:

$$I_A(N_1/N_2) = I_a + I_B(N_1/N_2) \rightarrow I_a = I_A(N_1/N_2) - I_B(N_1/N_2)$$

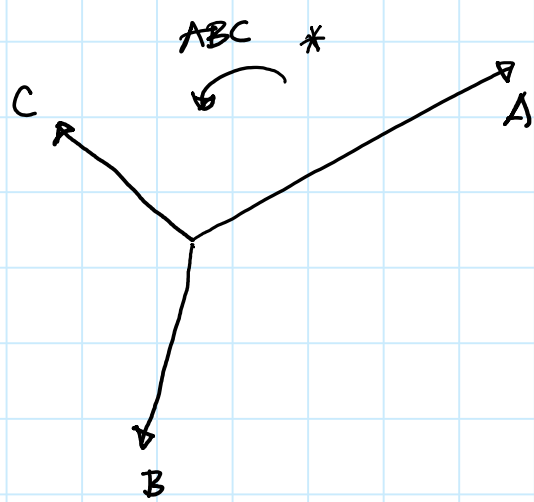
Using Wye phasor as reference:  $I_A = |I_A| \angle 90^\circ$ ;  $I_B = |I_A| \angle (90^\circ + 240^\circ)$

$$I_a = I_A(N_1/N_2) - I_B(N_1/N_2) = \sqrt{3} (N_1/N_2) |I_A| \angle 120^\circ$$

Conclusion:  $I_a$  lags  $I_a$  by  $30^\circ$  (Does not comply with IEEE)  
 we need to connect winding "a" of LV with winding "c" of HV.

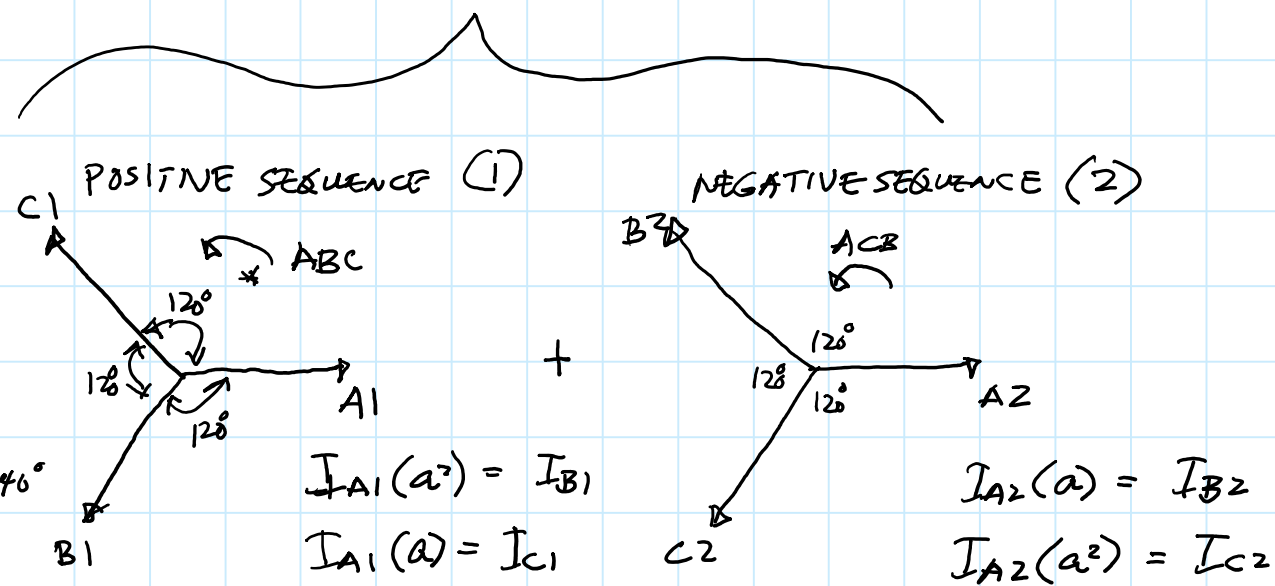
# Symmetrical Components

① Develop C.L. Fortescue - 1913

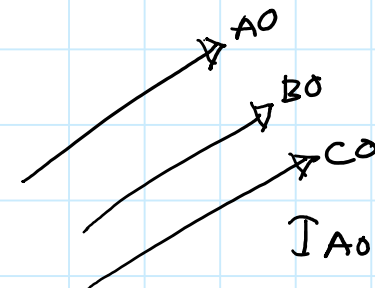


UNBALANCE  
ORIGINAL NETWORK  
PHYSICAL DOMAIN

## SEQUENCE DOMAIN



ZERO-SEQUENCE (0)



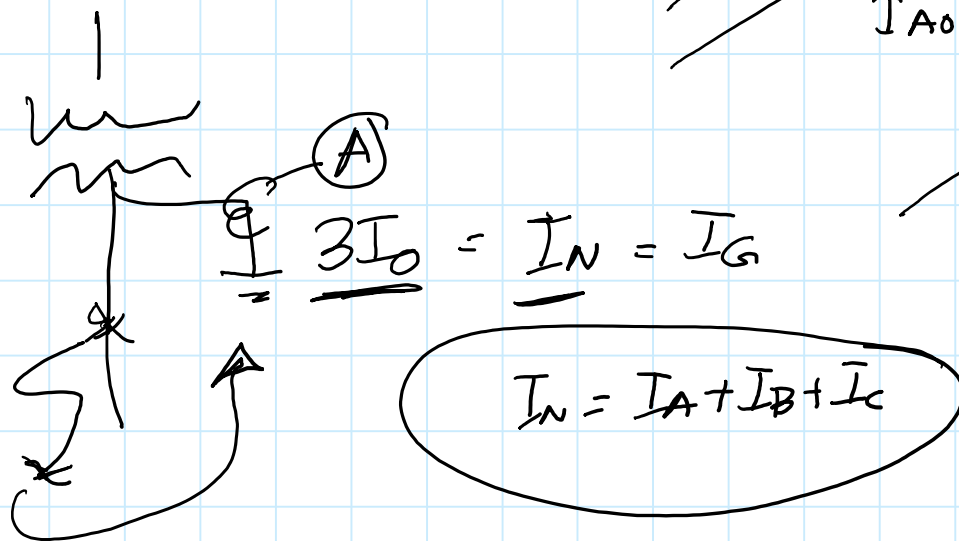
"a" operator =  $1 \angle 120^\circ$

$$I_{A0} = I_{B0} = I_{C0} \quad (V_{A0} = V_{B0} = V_{C0})$$

$$A0 = B0 = C0$$

$$1 \angle 120^\circ = a$$

$$1 \angle 240^\circ = a^2$$



$$\begin{aligned} \textcircled{1} \quad I_A &= I_{A1} + I_{A2} + I_{A0} = I_{A1} + I_{A2} + I_{A0} \\ \textcircled{2} \quad I_B &= I_{B1} + I_{B2} + I_{B0} = a^2 I_{A1} + a I_{A2} + I_{A0} \\ \textcircled{3} \quad I_C &= I_{C1} + I_{C2} + I_{C0} = a I_{A1} + a^2 I_{A2} + I_{A0} \end{aligned}$$

Dropping the "A" subscript

$$\begin{aligned} &= I_1 + I_2 + I_0 \\ &= a^2 I_1 + a I_2 + I_0 \times a^2 \\ &= a I_1 + a^2 I_2 + I_0 \times a \end{aligned}$$

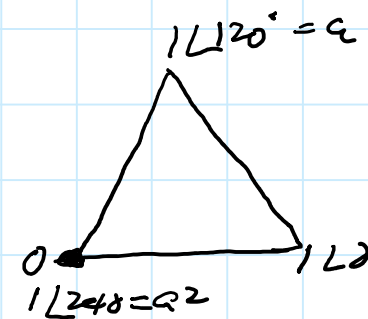
SOLVING FOR ZERO-SEQUENCE CURRENT:

$$\textcircled{1} + \textcircled{2} + \textcircled{3}$$

$$I_A + I_B + I_C = I_1(1 + a^2 + a) + I_2(1 + a + a^2) + I_0(1 + 1 + 1)$$

$$3I_0 = I_A + I_B + I_C$$

$$1 + a + a^2 = 0$$



SOLVING FOR POSITIVE-SEQUENCE CURRENT:

$$\begin{aligned} I_A + a I_B + a^2 I_C &= I_1(1 + a^3 + a^3) + I_2(1 + a^2 + a^4) + I_0(1 + a + a^2) \\ &= I_1(1 + 1 + 1) + I_2(1 + a^2 + a) + I_0(1 + a + a^2) \end{aligned}$$

$$3I_1 = I_A + a I_B + a^2 I_C$$

$$a^3 = (1 \angle 120^\circ)^3$$

$$= 1^3 \angle 3 \times 120$$

$$= 1 \angle 360 = 1 \angle 0$$

SOLVING FOR NEGATIVE-SEQUENCE CURRENT:

$$I_A + a^2 I_B + a I_C = I_1(1 + a^4 + a^2) + I_2(1 + a^3 + a^3) + I_0(1 + a^2 + a)$$

$$3I_2 = I_A + a^2 I_B + a I_C$$

$$3I_0 = I_A + I_B + I_C$$

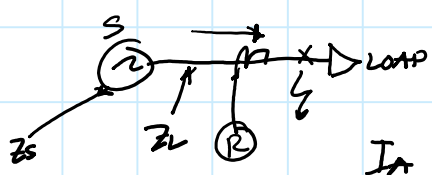
$$3I_1 = I_A + aI_B + a^2I_C$$

$$3I_2 = I_A + a^2I_B + aI_C$$

$$I_A = I_1 + I_2 + I_0$$

$$I_B = a^2I_1 + aI_2 + I_0$$

$$I_C = aI_1 + a^2I_2 + I_0$$

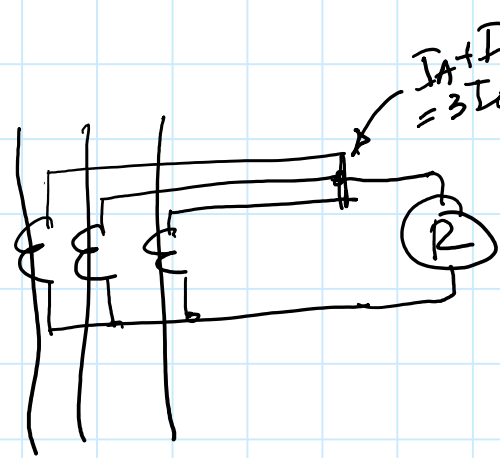


$$\begin{bmatrix} I_0 \\ I_1 \\ I_2 \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & 1 & 1 \\ 1 & a & a^2 \\ 1 & a^2 & a \end{bmatrix} \begin{bmatrix} I_A \\ I_B \\ I_C \end{bmatrix}$$

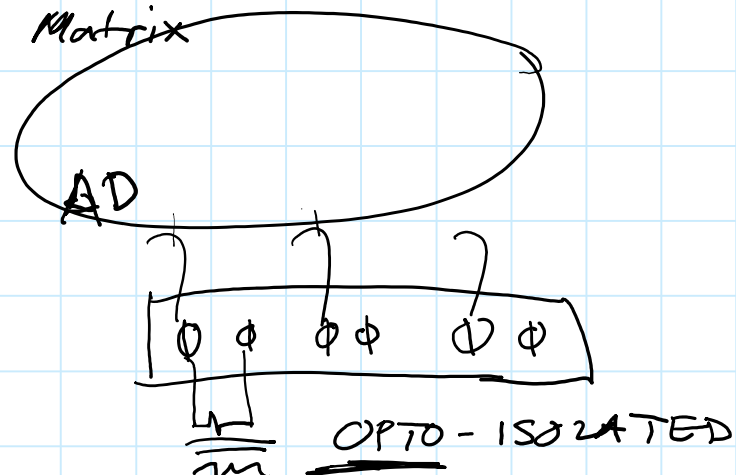
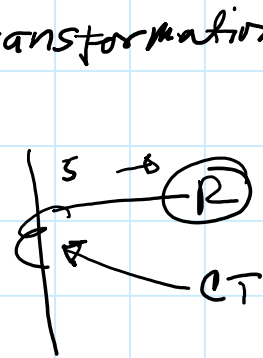
$$\begin{bmatrix} I_A \\ I_B \\ I_C \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ a^2 & a & 1 \\ a & a^2 & 1 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_0 \end{bmatrix}$$

$$[I_s] = \frac{1}{3} [A^{-1}] [I_p]$$

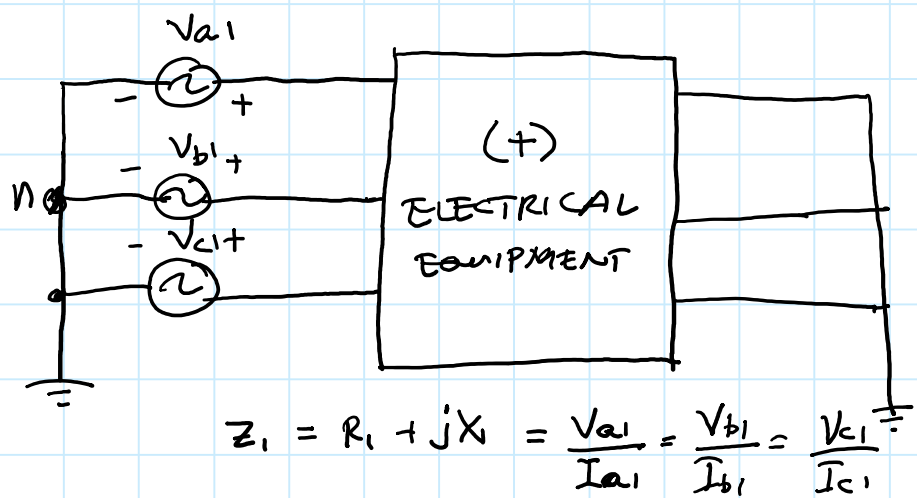
$$[I_p] = [A] [I_s]$$



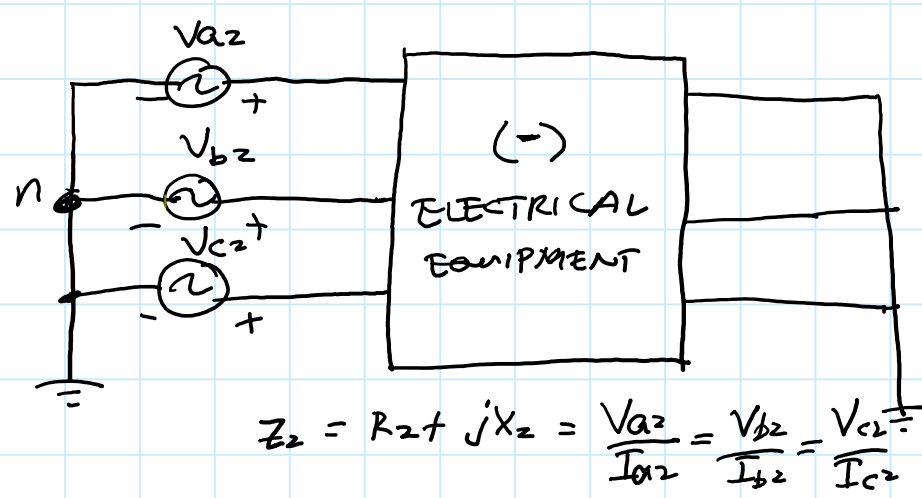
$I_A + I_B + I_C = 3I_0$  [A] = Transformation Matrix



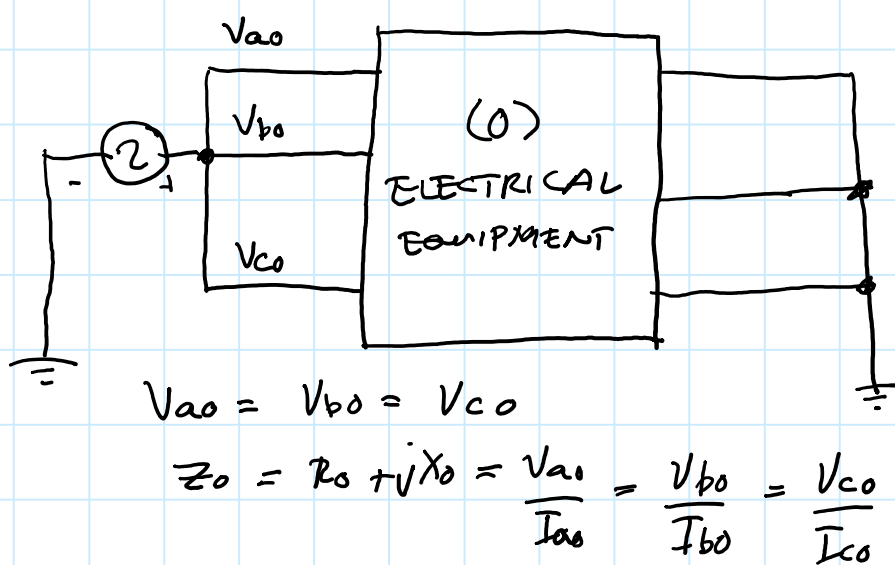
### POSITIVE-SEQUENCE TEST



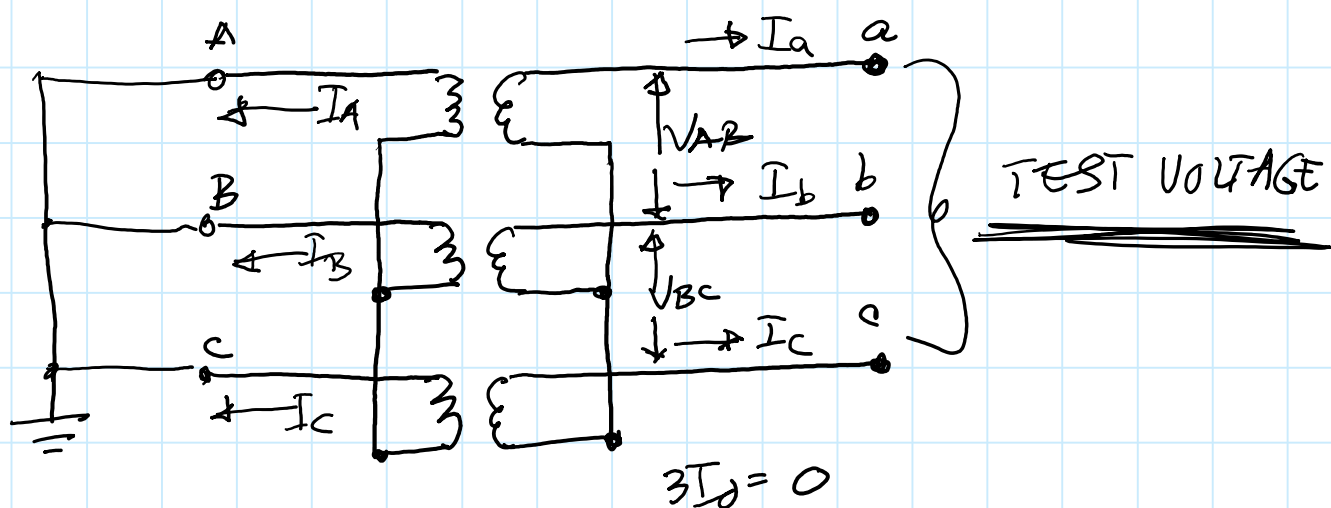
### NEGATIVE-SEQUENCE TEST



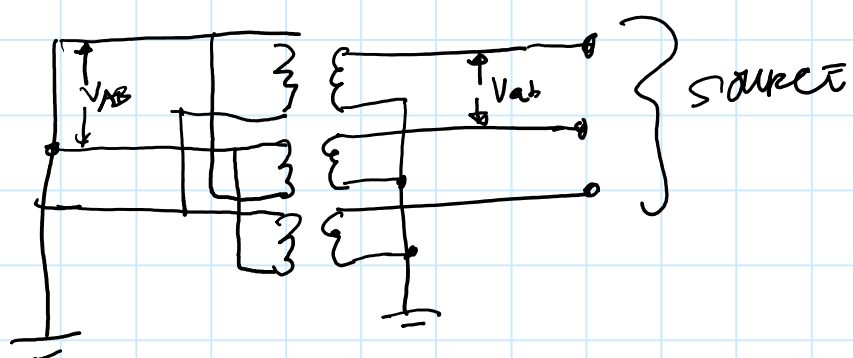
### ZERO-SEQUENCE TEST



### Wye-Wye Transformer



### Delta-Wye Transformer



$$V_A = 1 \angle 0^\circ$$

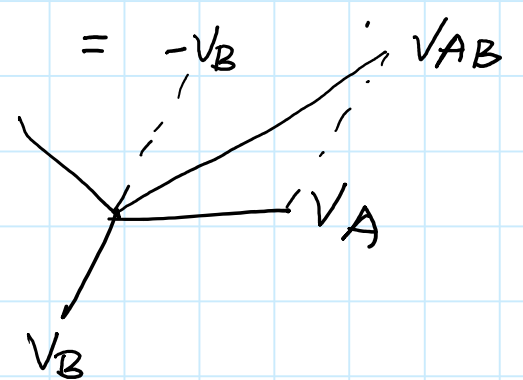
$$V_B = 1 \angle 240^\circ$$

$$V_C = 1 \angle 120^\circ$$

$$V_A = \sqrt{3} \angle 30^\circ$$

$$V_{AB} = V_A - V_B$$

$$= -V_B$$

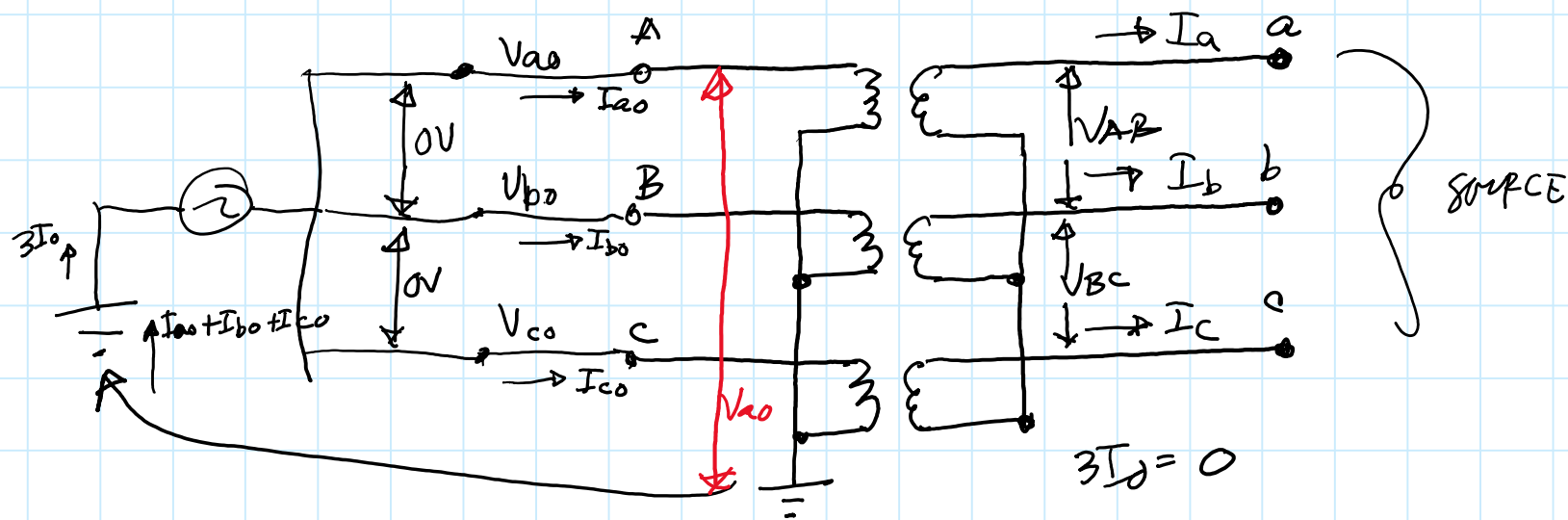




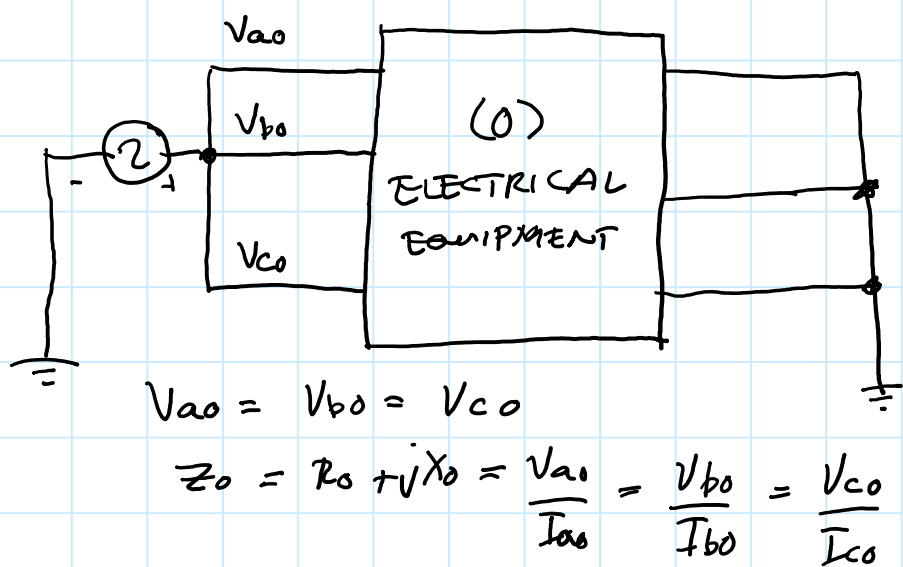
$\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$

$\frac{1}{2}$

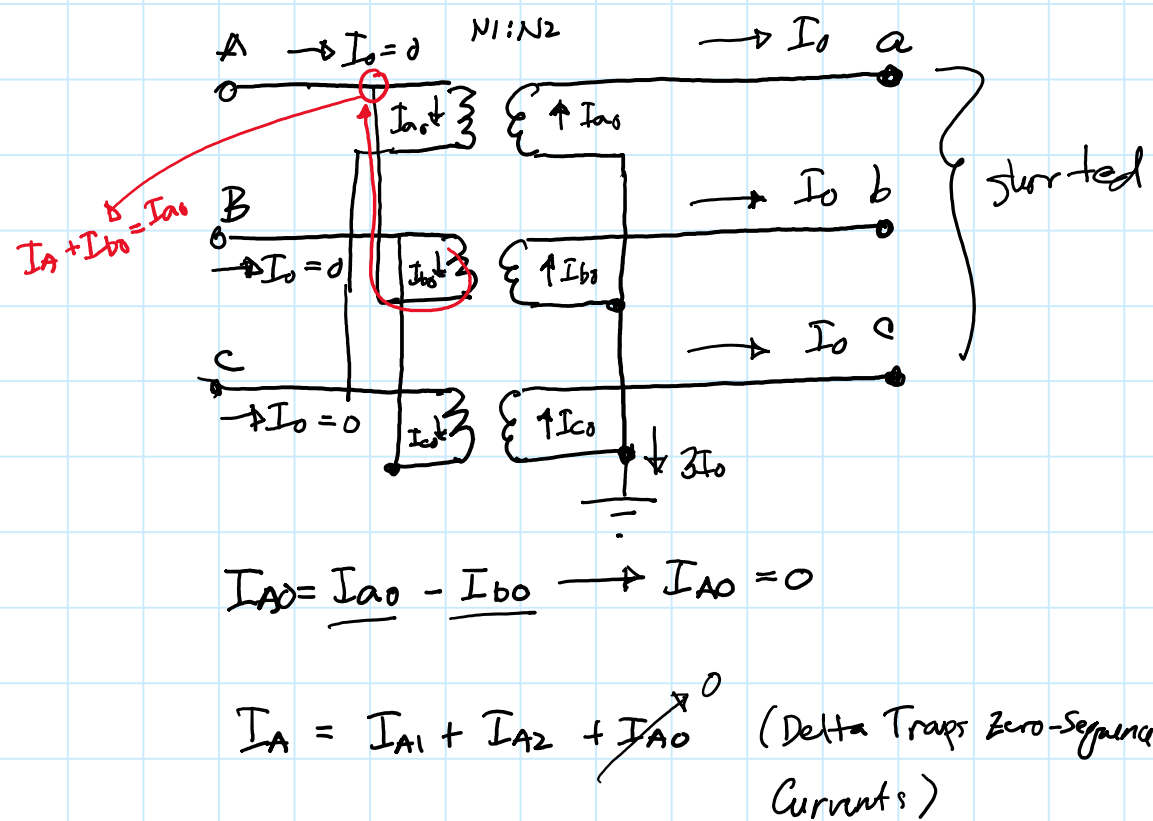
# Wye-Wye Transformer (Zero-Sequence Test)



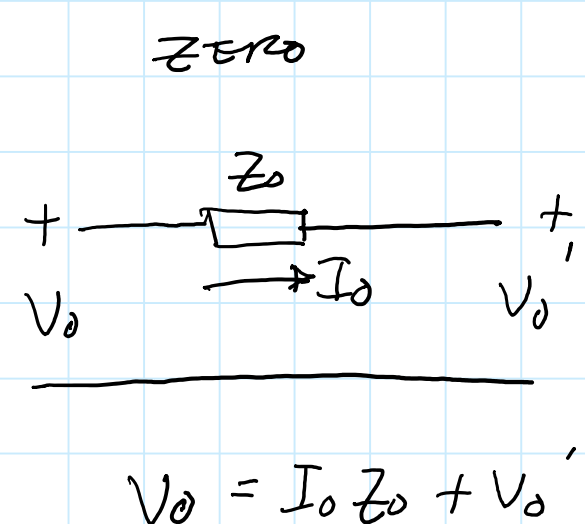
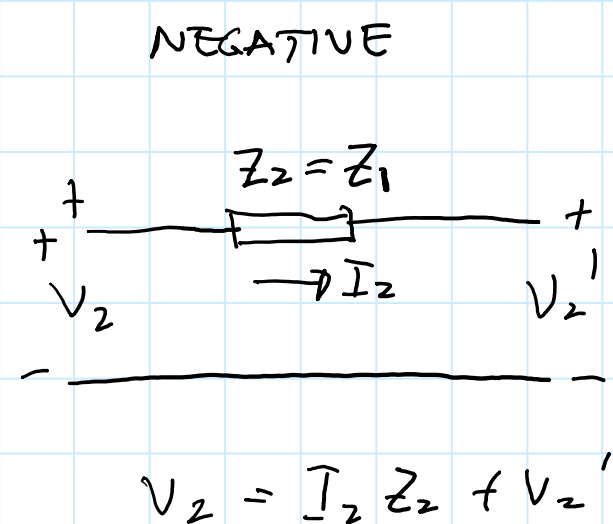
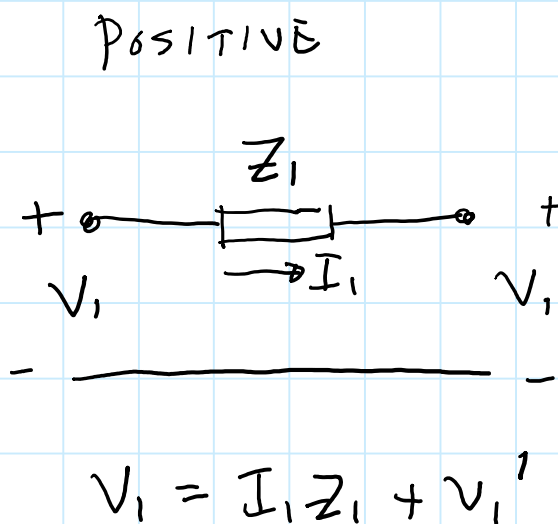
## ZERO-SEQUENCE TEST



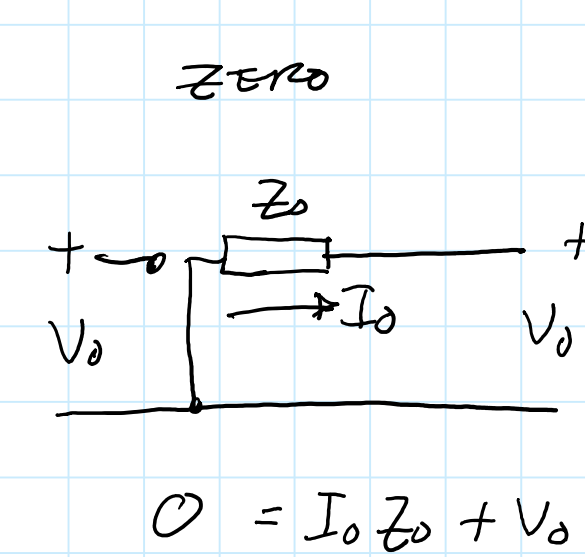
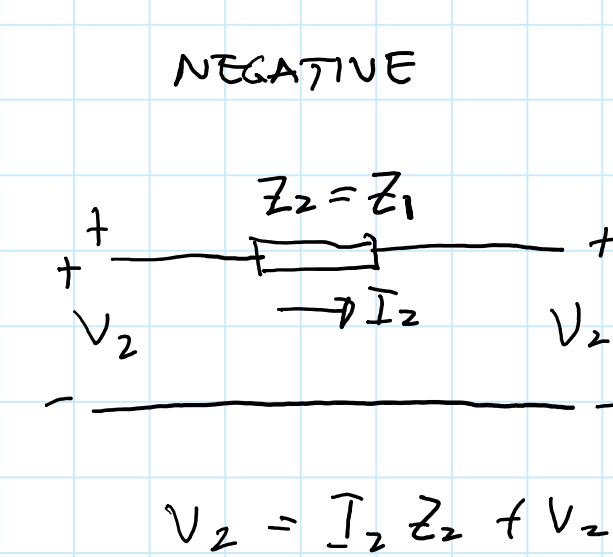
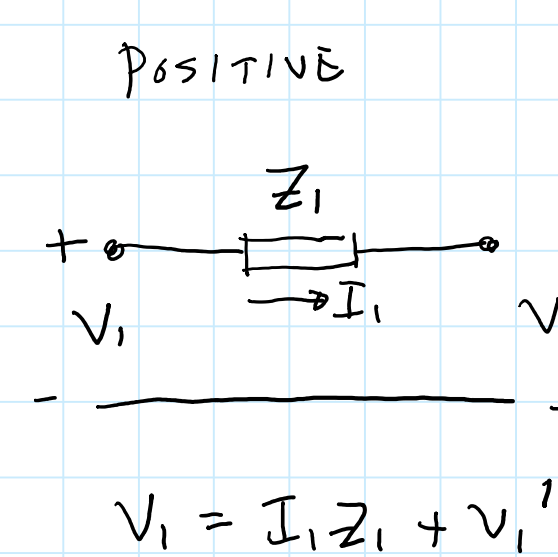
## Delta-Wye Transformer



## SEQUENCE NETWORK OF WYE-WYE TRANSFORMER



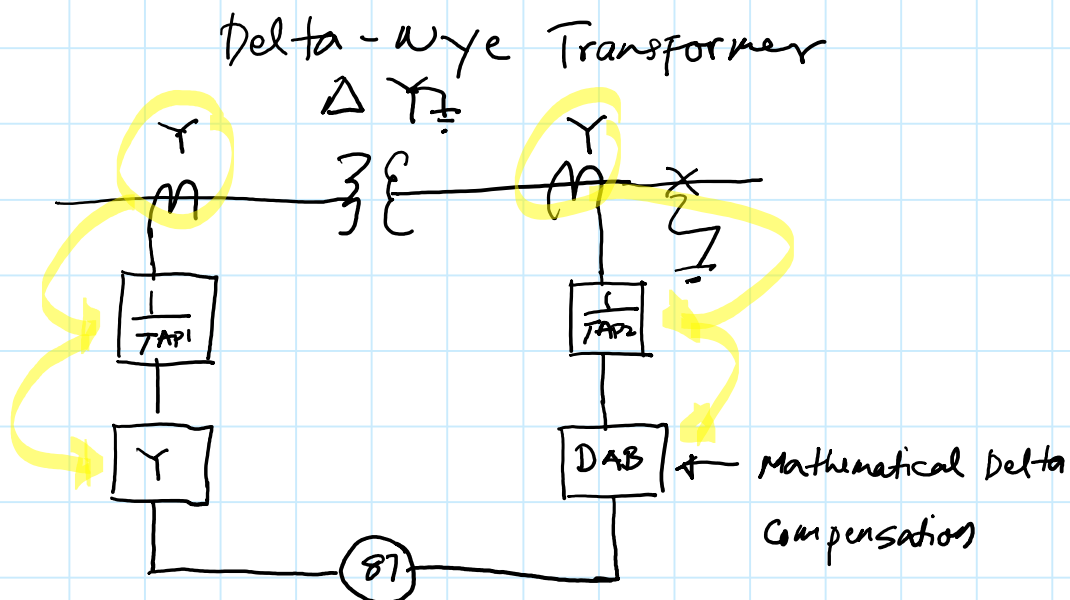
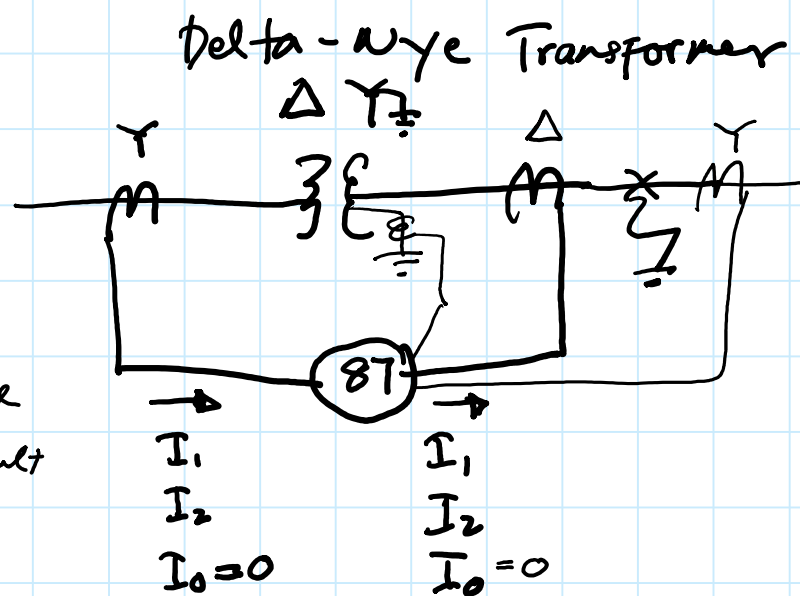
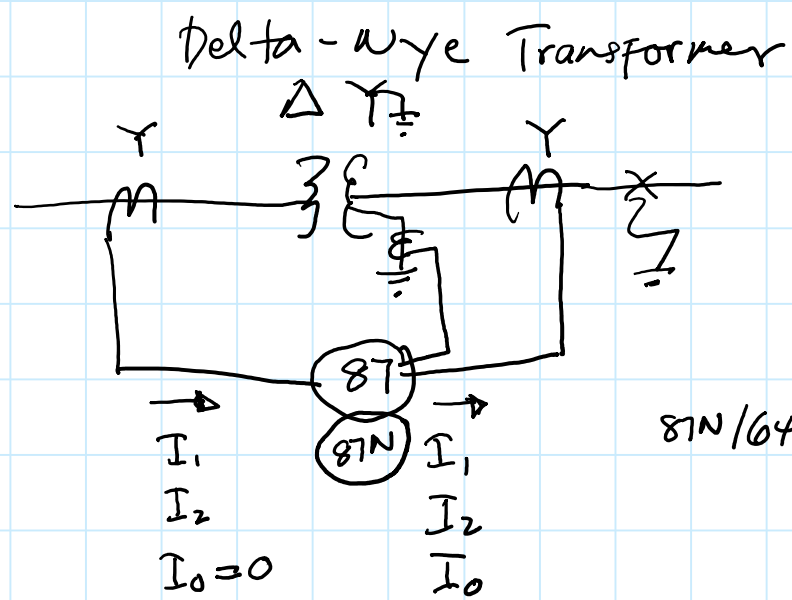
## SEQUENCE NETWORK OF DELTA-WYE TRANSFORMER



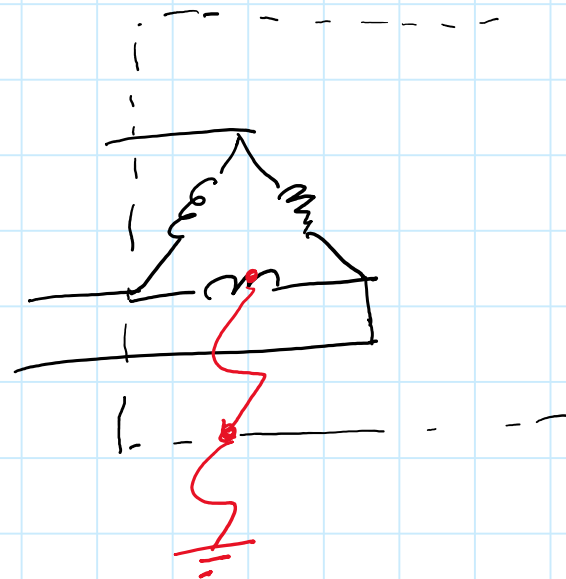
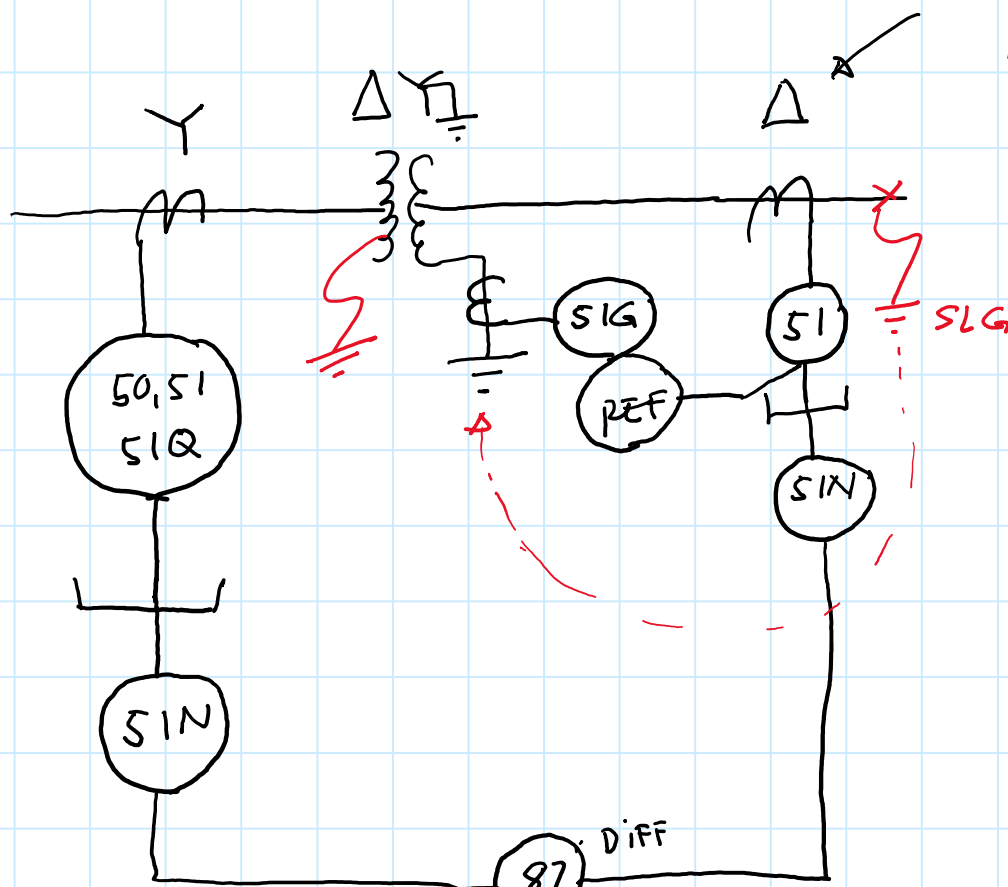
$$V_1 = I_1 Z_1 + V_1'$$

$$V_2 = I_2 Z_2 + V_2'$$

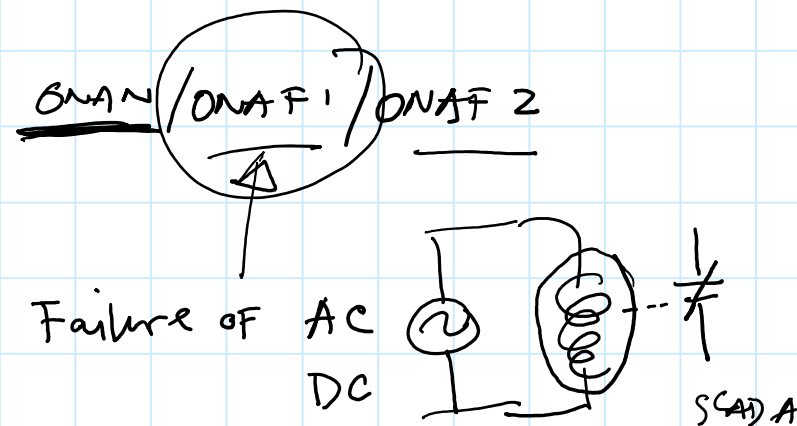
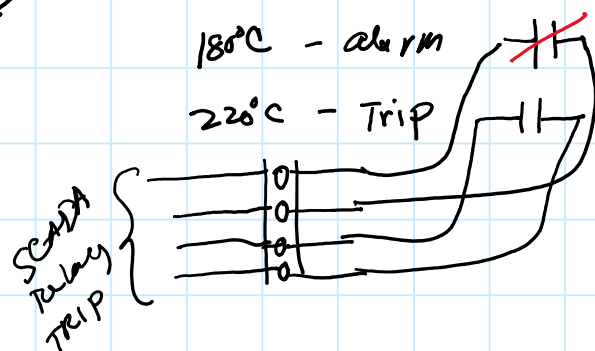
$$V_0 = I_0 Z_0 + V_0'$$

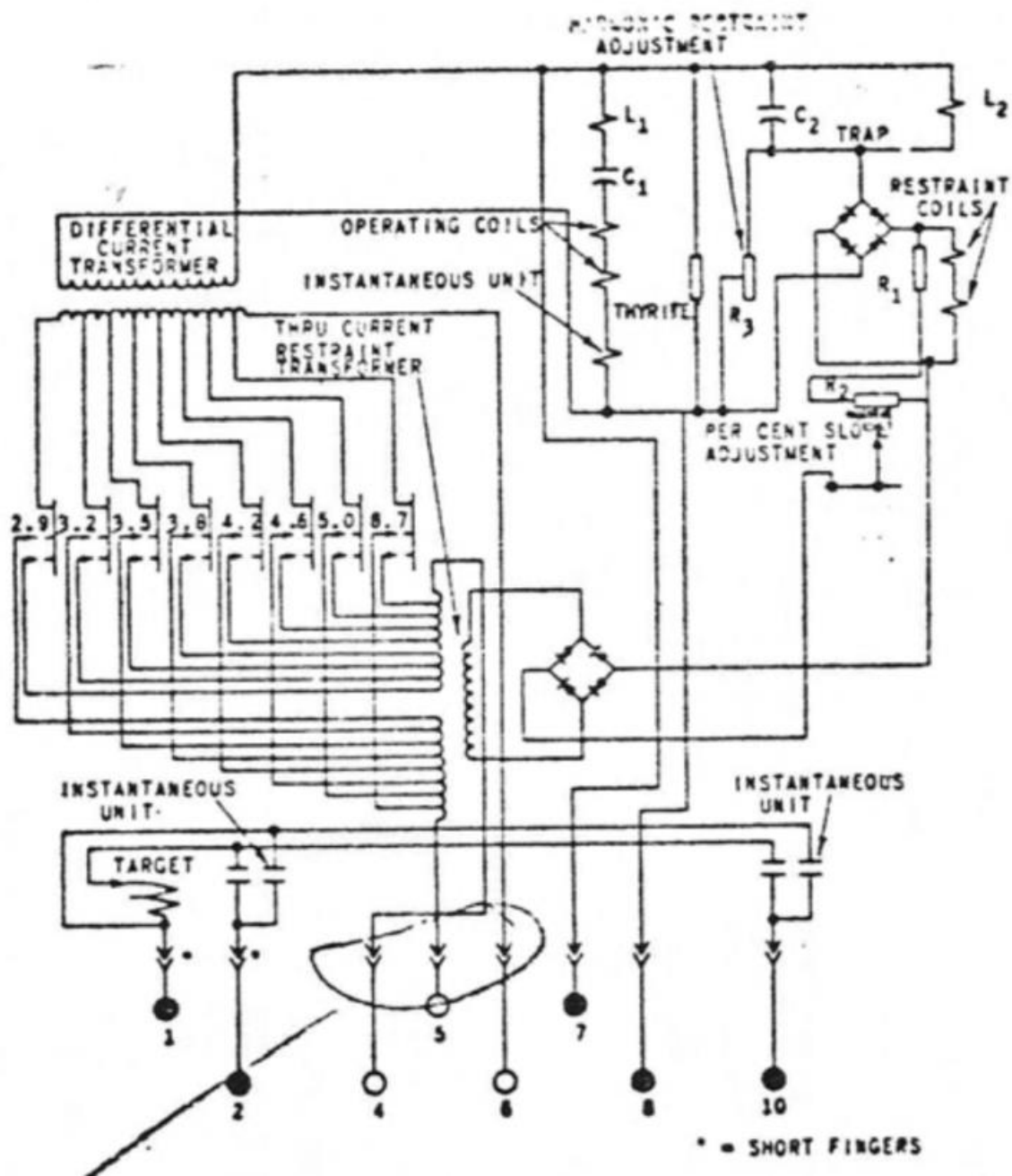
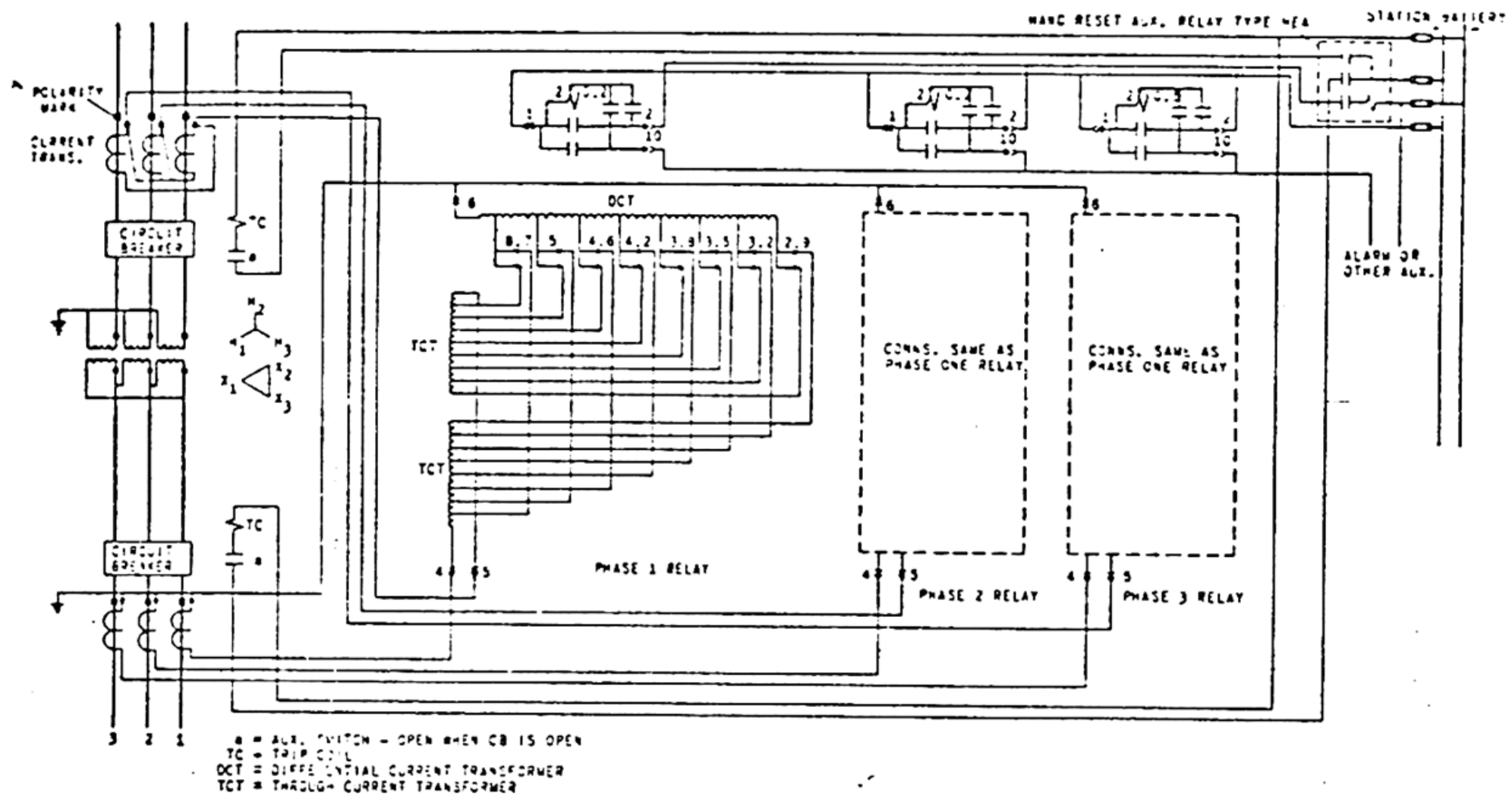


To be connected Delta when using EM Relay.  
Recommended to be connected Wye when using Numerical Relay

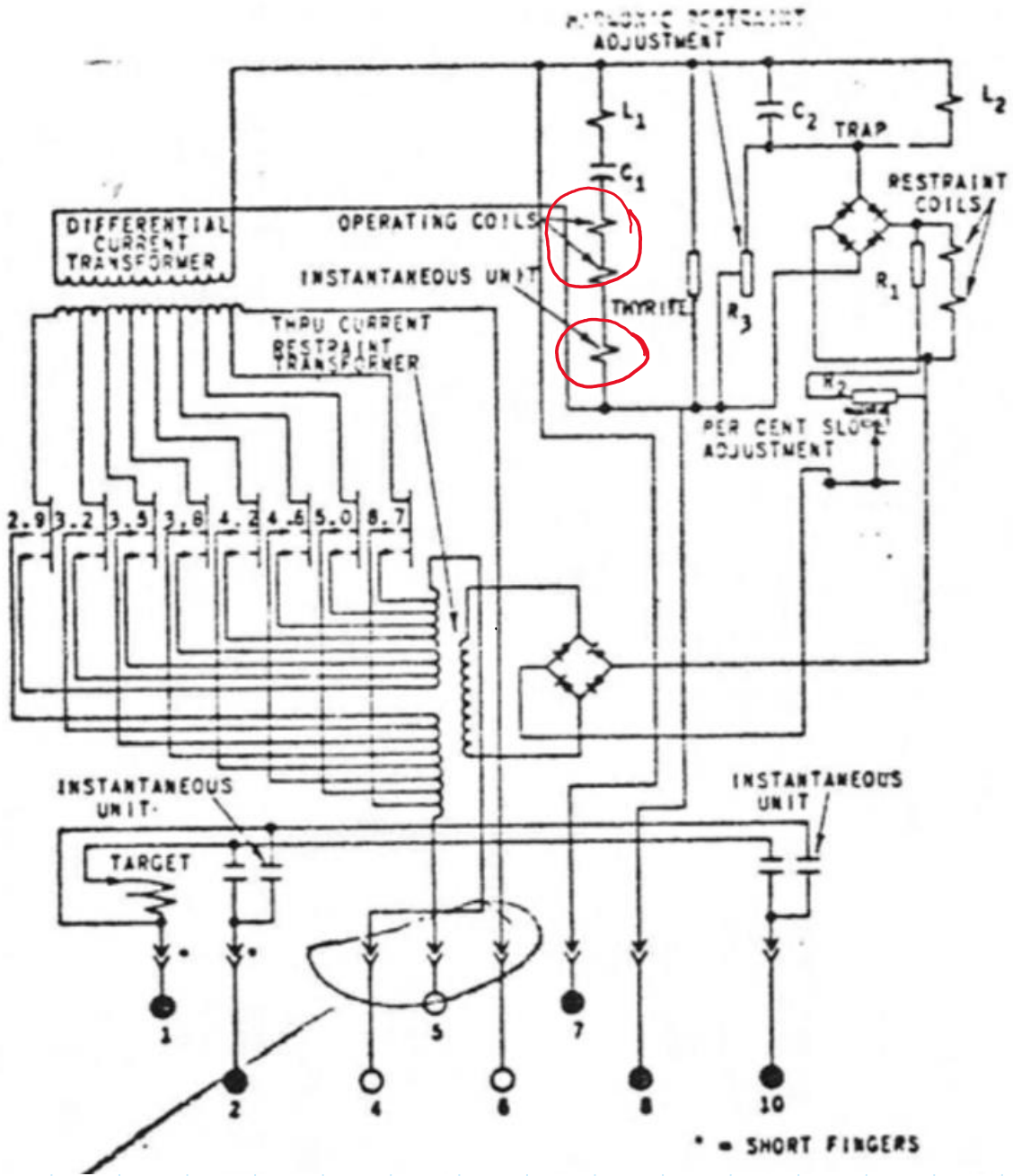
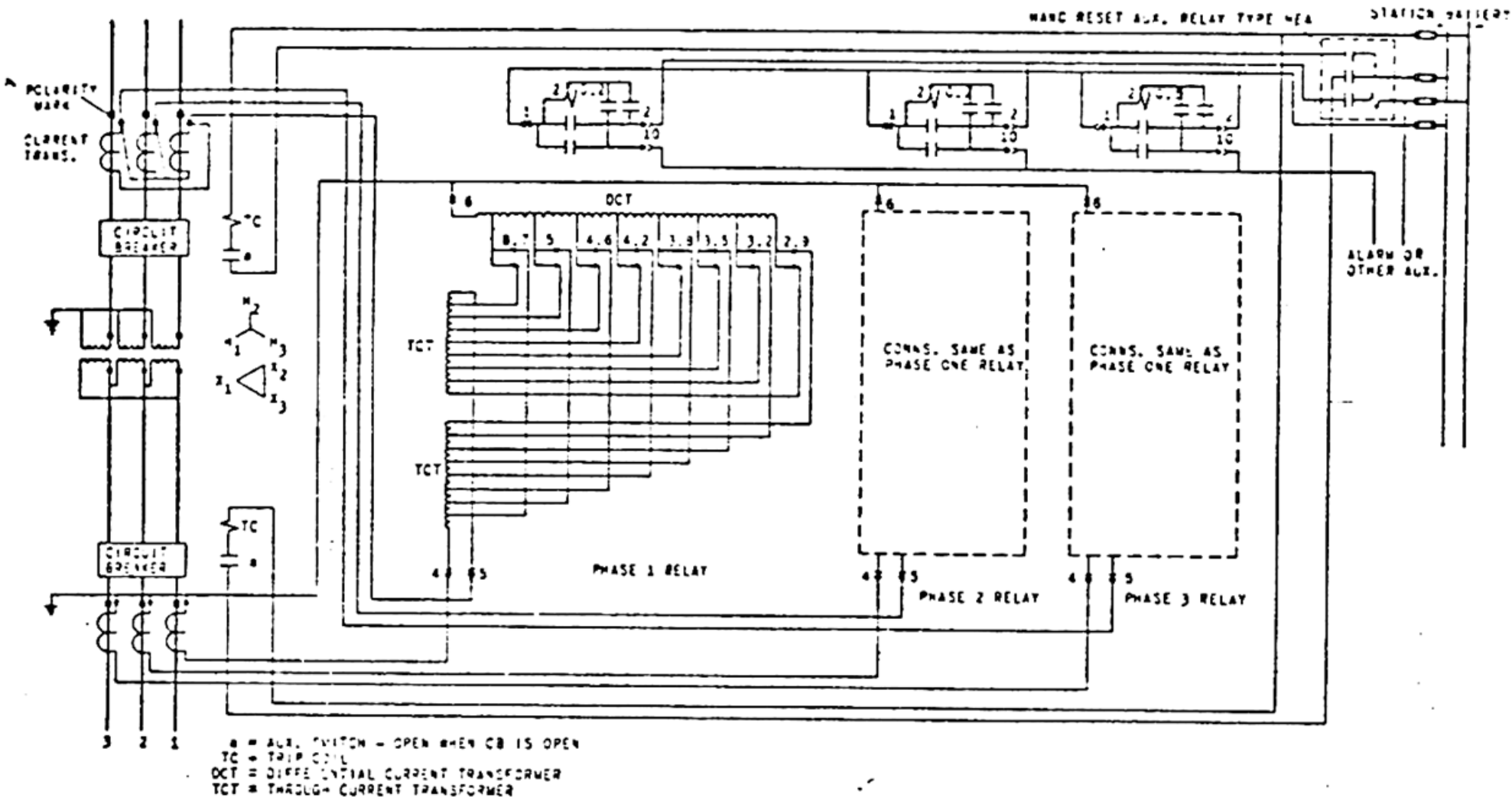


- 24 V/Hz
- 59 OV
- 63 Sudden Pressure (Rapid Rise Pressure Relay) ✓
- 49 Thermal (RTD, WDG CT) - Typically Two Stages (Alarm and Trip)





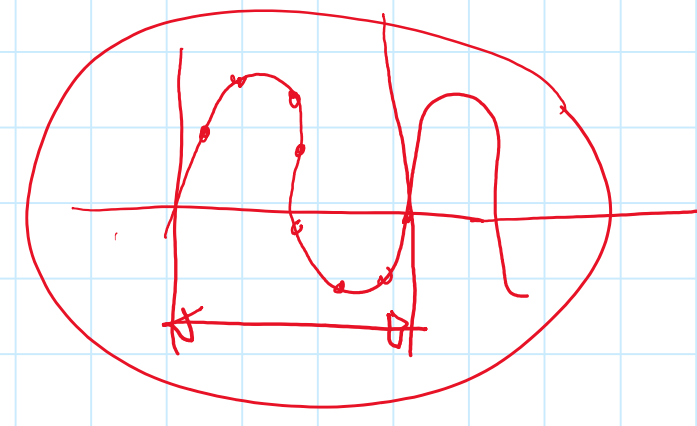


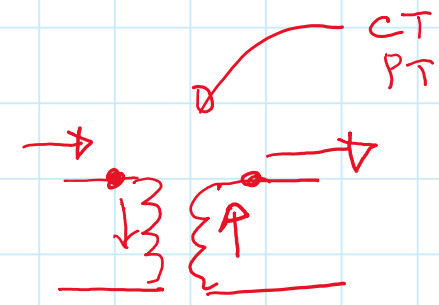
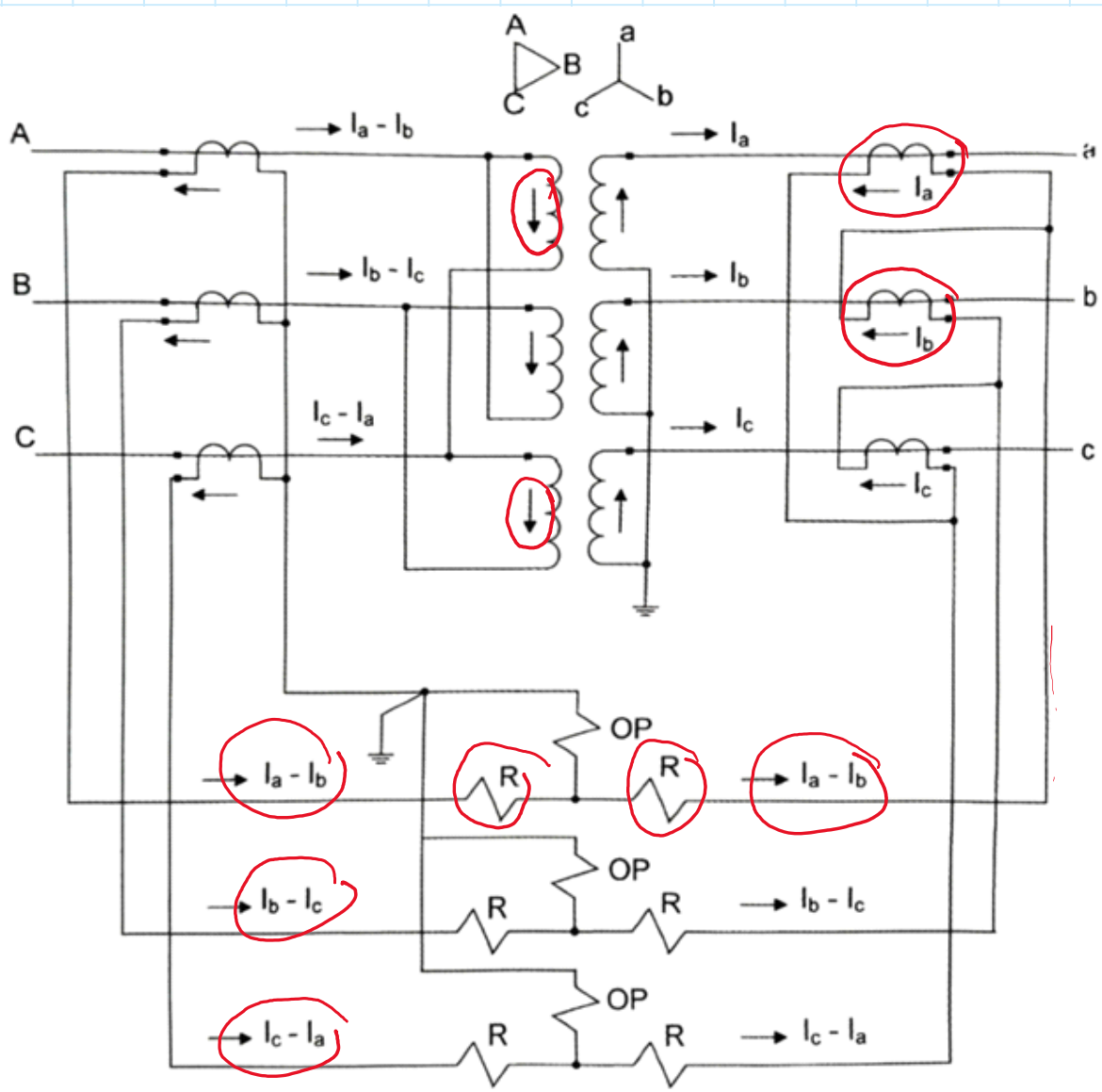


$L_1$  } respond to fundamental  
 $C_1$  }

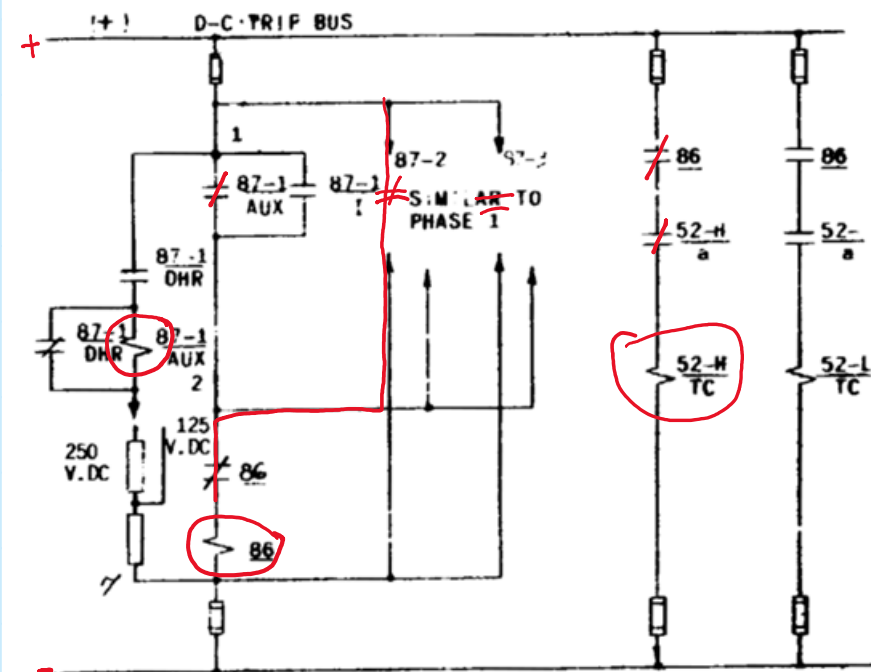
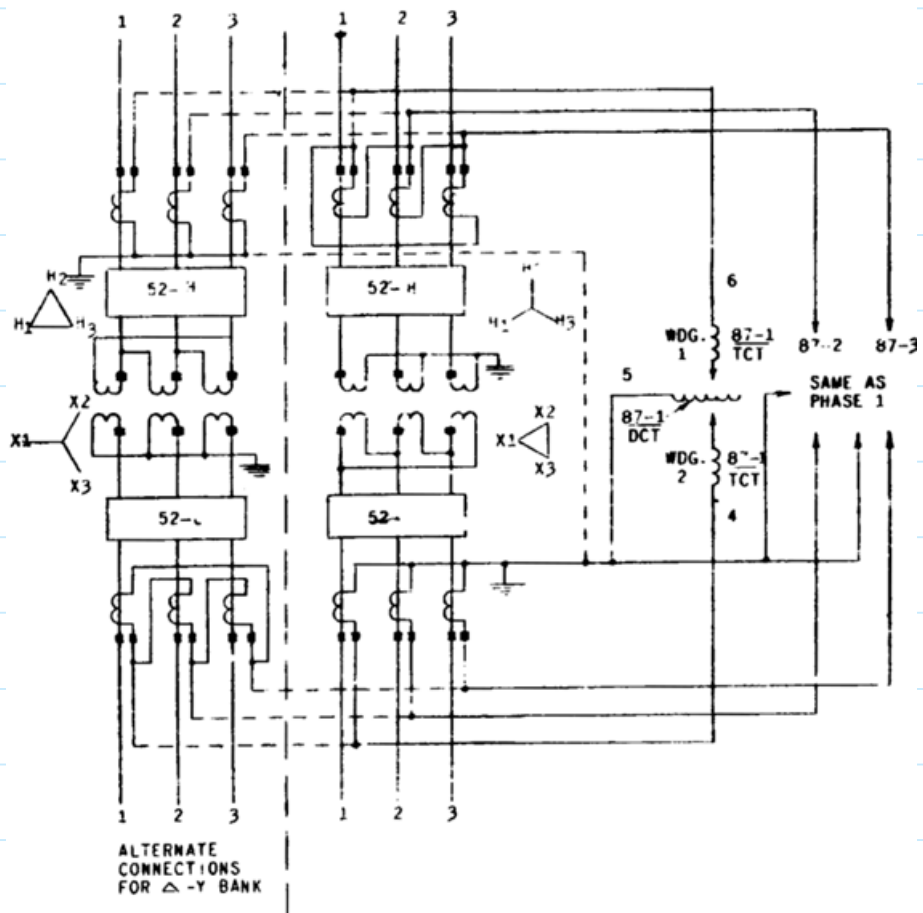
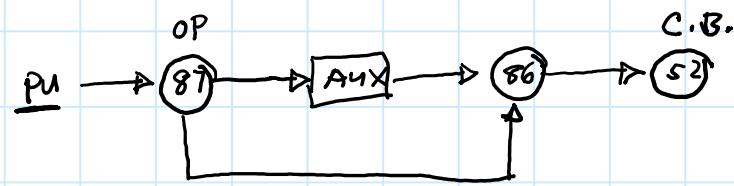
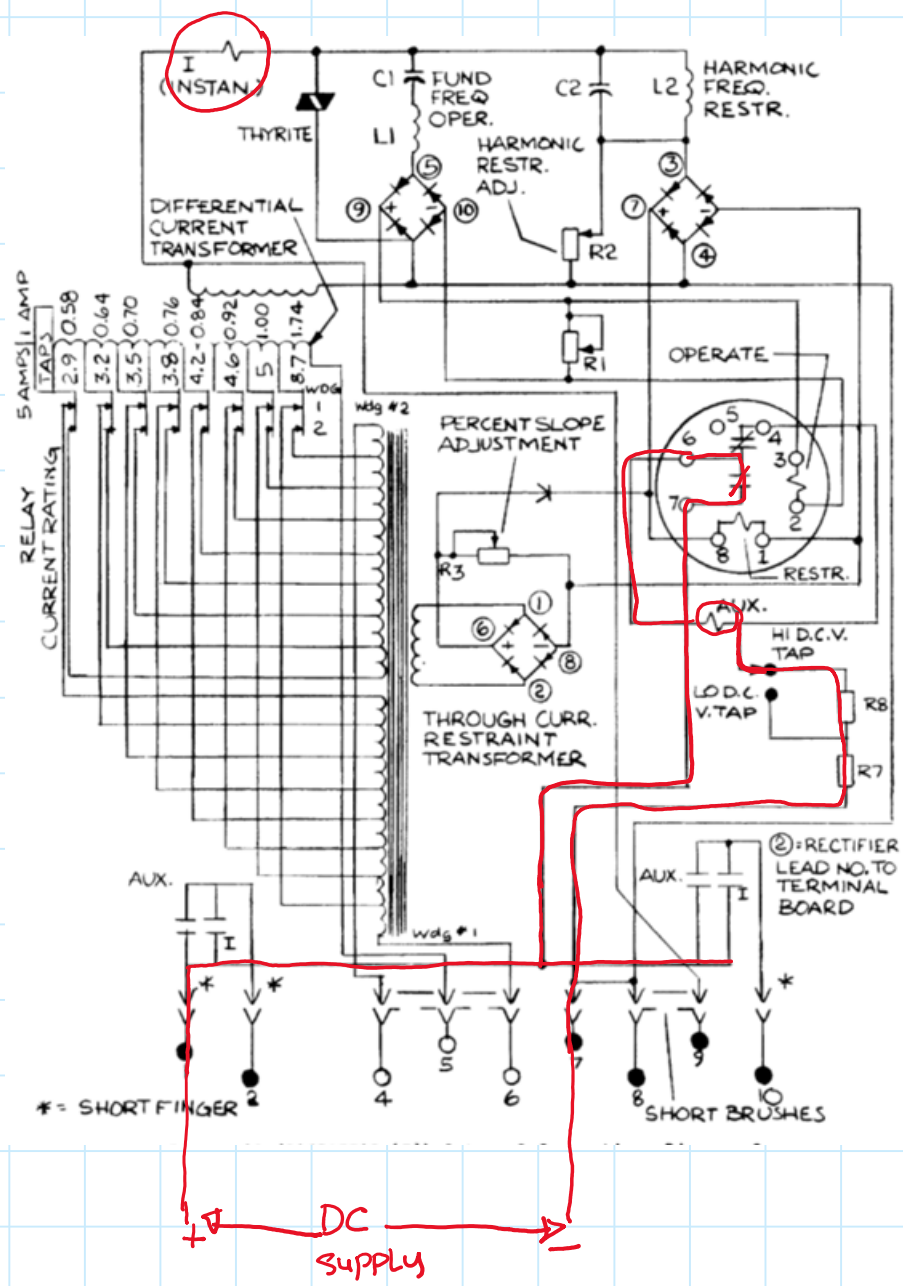
$L_2$  } Trap / Reject Fundamental  
 $C_2$  } Respond to Harmonics

sample/cycle  
 $16 \times 60 = 960$  samples/sec  
 $\uparrow$   
 60Hz  $1/60$  sec

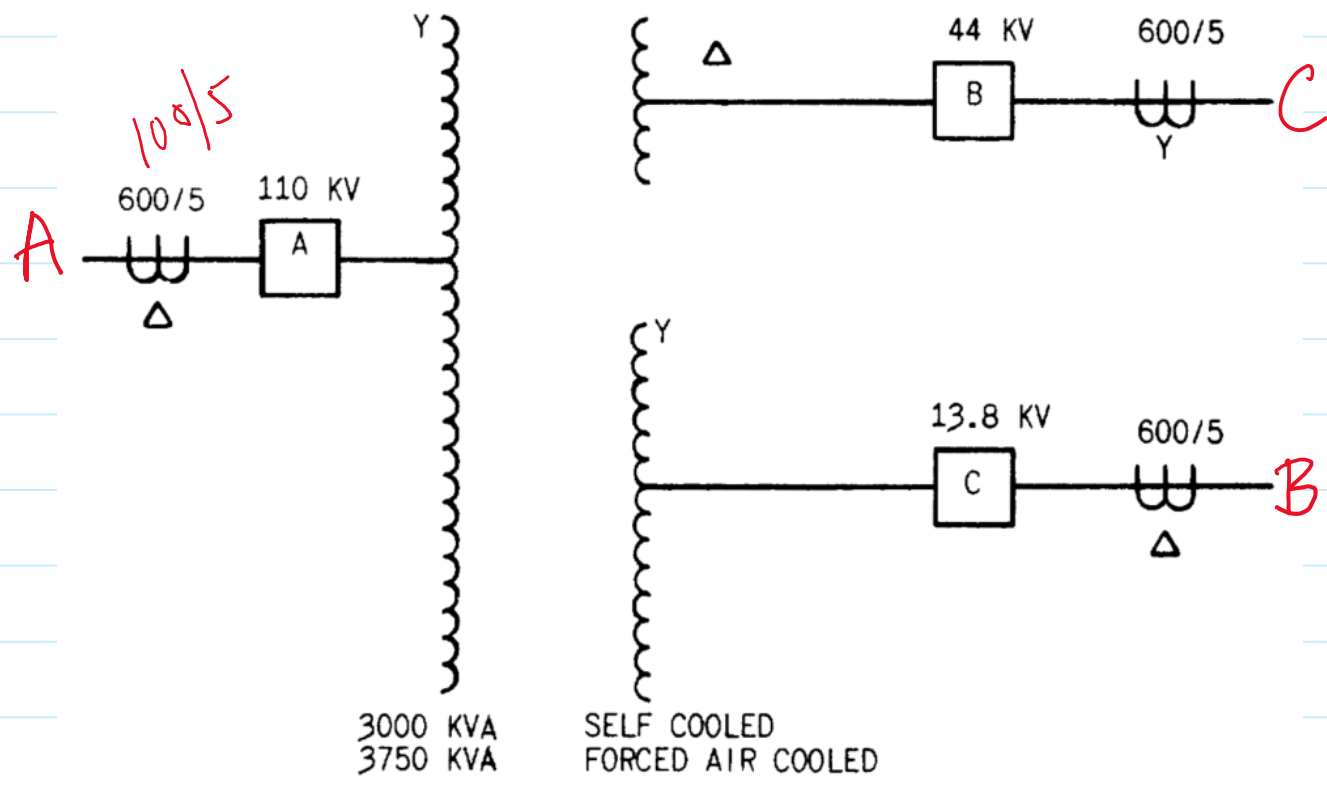




Restraining characteristics (External Fault)  
Digital Relay



- a = AUX. SWITCH, OPEN WHEN BREAKER IS OPEN
- TC = TRIP COIL
- DCT = DIFFERENTIAL CURRENT TRANSFORMER
- TCT = THROUGH CURRENT TRANSFORMER
- I = INSTANTANEOUS OVERCURRENT
- DHR = DIFFERENTIAL UNIT WITH HARMONIC RESTRAINT
- 86 = HAND RESET RELAY TYPE HEA
- 52 = POWER CIRCUIT BREAKER
- 87 = TYPE BOD DIFFERENTIAL RELAY



WYE-WYE-DELTA

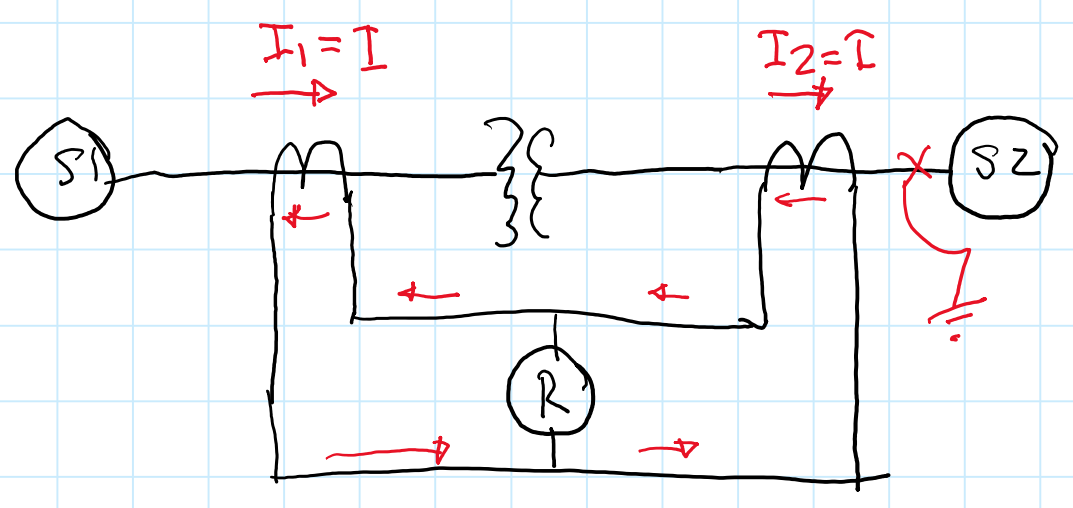
$$E_s = CN / 20$$

$$I_e = D / 20N$$

OIL CIRCUIT BREAKER		BUSHING CURRENT TRANSFORMERS				
Type	RATING		CONSTANTS		INTERNAL RESISTANCE	
	KV	Amperes	C	D	Ohms per Turn	Ohms per Lead*
FK-339	15	1600-4000	19	700	.0035	.025
	23	600-1200	11	450	.003	.025
	23	2000	19	700	.0035	.03
	34.5	600-1200	12	400	.003	.035
	34.5	2000-3000	21	800	.0035	.035
	46	600-1200	14	550	.003	.035
	69	600-1200	28	1100	.004	.04
	115	600-1200	45	1700	.0035	.05
	138	600-1200	53	2000	.0035	.06
	161	600-1200	58	2300	.0035	.08
	230/196	600-1200	65	2500	.007	.1
	230	600-1200	65	2500	.007	.1

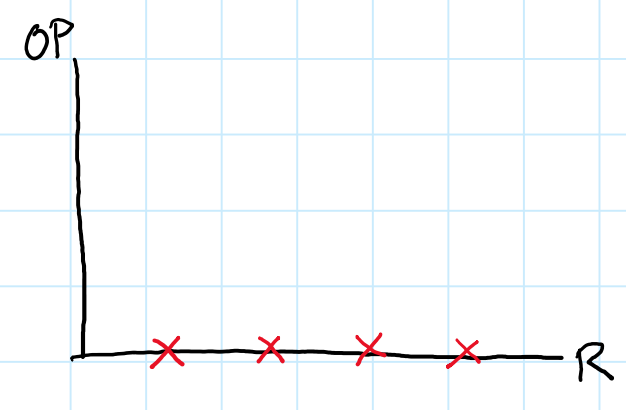


Restraining Characteristics (External Fault)  
Digital Relay

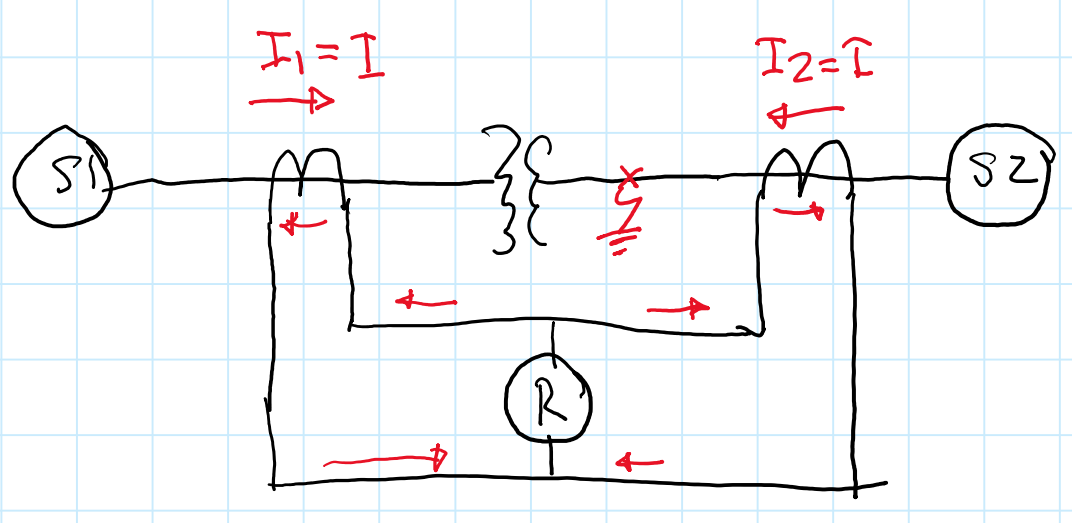


Relay Operating Current =  $I_1 - I_2 = 0$

Relay Restraining Current =  $[I_1] + [I_2] = 2I$

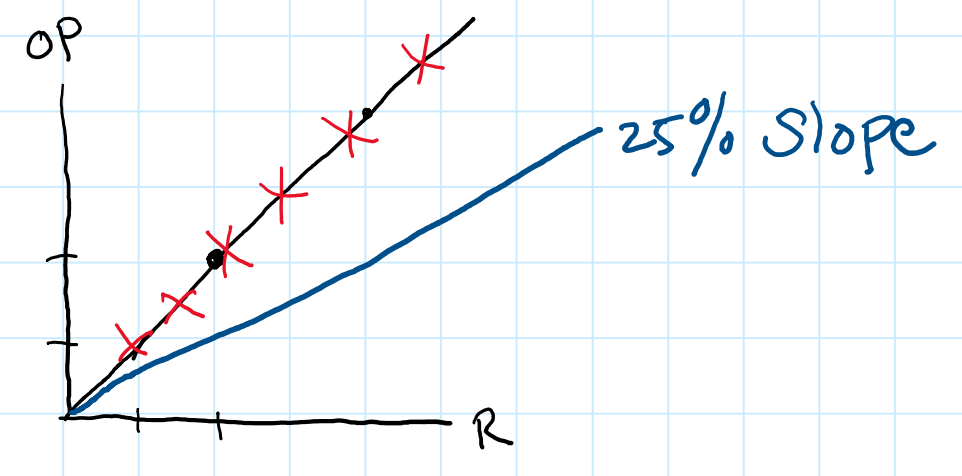


Restraining Characteristics (Internal Fault)  
Digital Relay



Relay Operating Current =  $I_1 - I_2 = I - (-I) = 2I$

Relay Restraining Current =  $[I_1] + [I_2] = I + I = 2I$



Percentage Slope is determined by the sum of:

- ① Load control range (LTC) ←
- ② Mismatch of the relay taps ←



# ANSI/IEEE Relay Current Transformers

Up to 10% Error at 20 times rated current

Let's say 1200/5 CT, then the 20 times rated current is  $20 \times 5A = \underline{100A}$

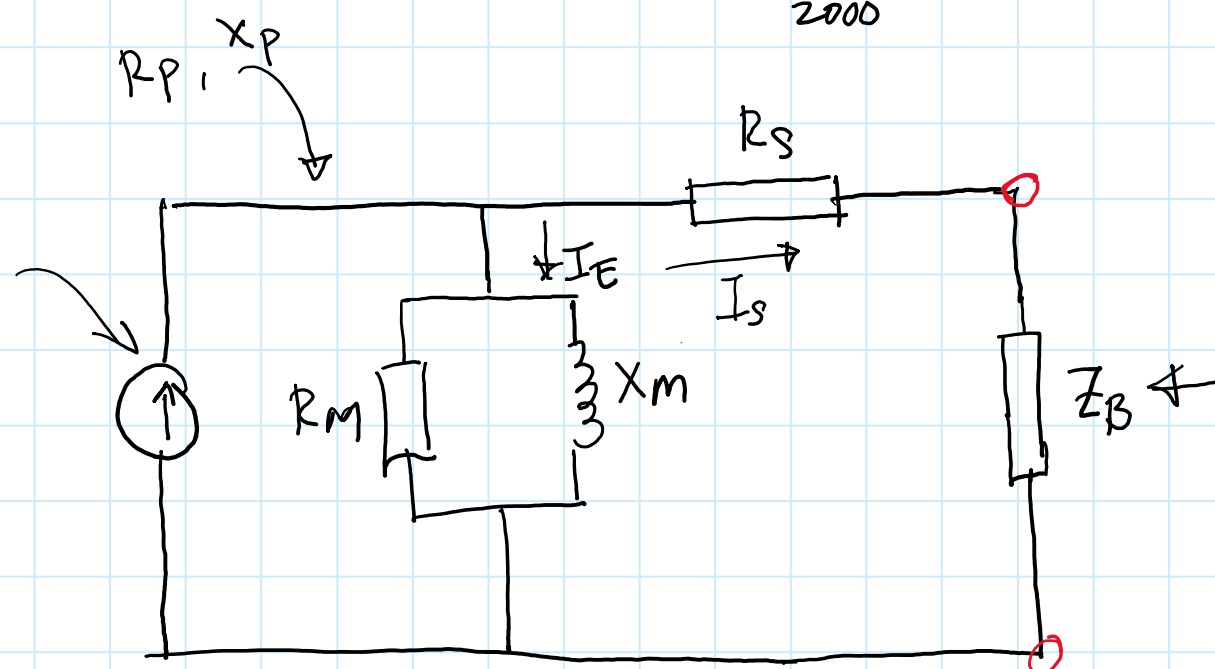
class	$Z_B$ STD ( $\Omega$ )	V STD (V)
C100	1	100
C200	2	200
C400	4	400
C800	8	800

$$100 / 100 = 1\% \text{ error}$$

## Tapping a CT

2000:5, C800 tapped at 1200:5

$$\text{Effective Voltage} = 800 \times \frac{1200}{2000} = 480V$$



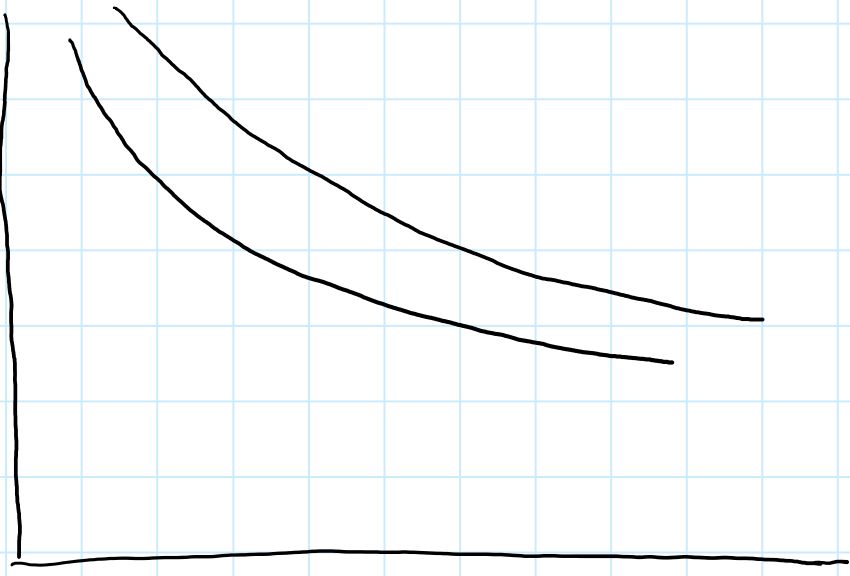
$$\text{CT Composite Error} = \frac{I_e}{I_s}$$

For a 100A secondary current:

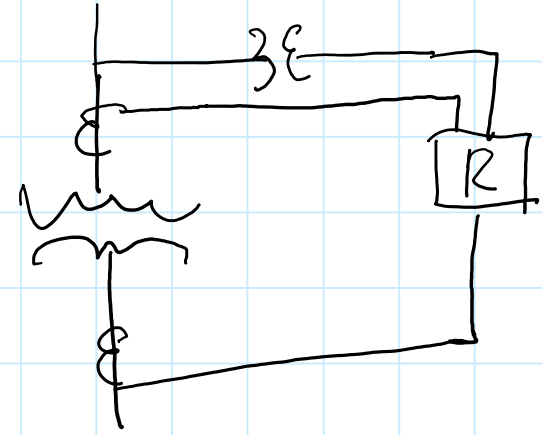
$$I_e = 10A$$

$$I_s = 90A$$

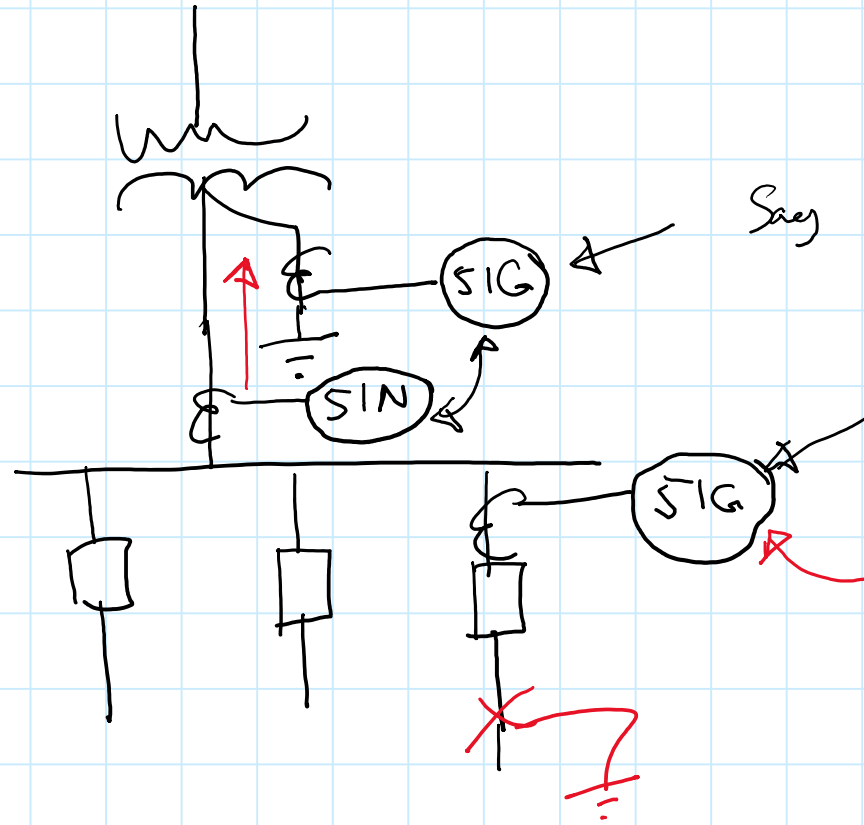
1.4



V/Hz



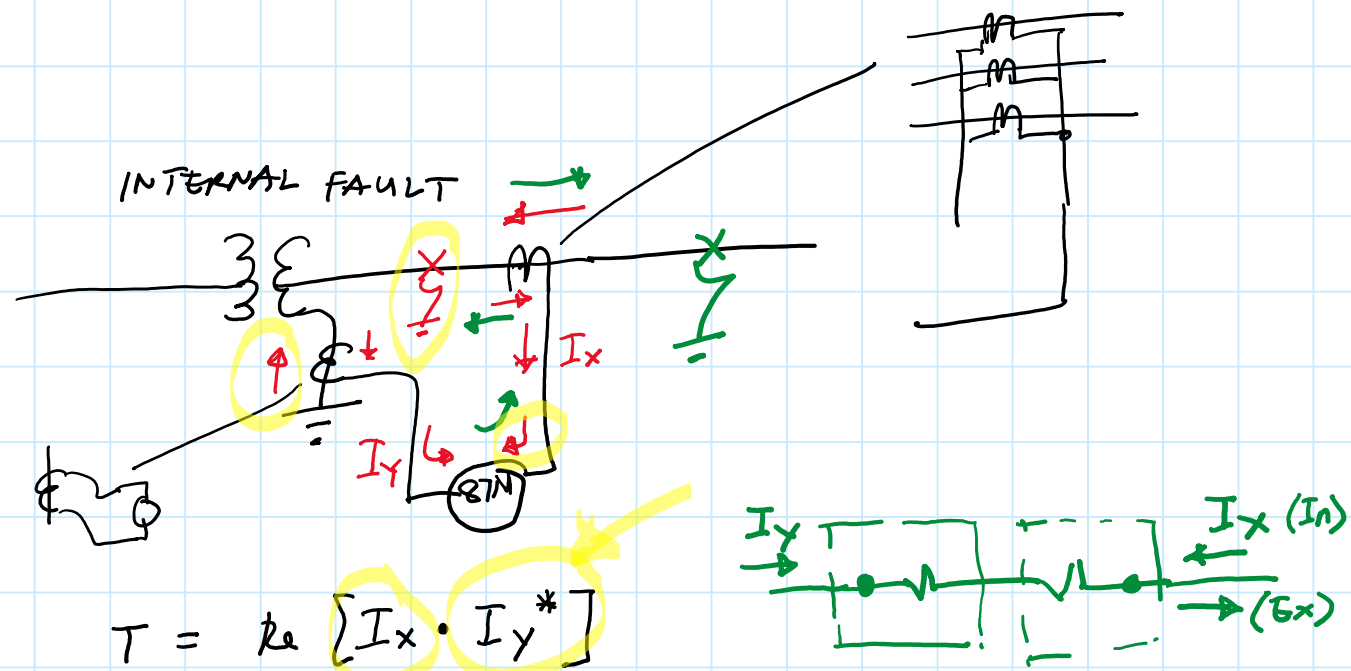
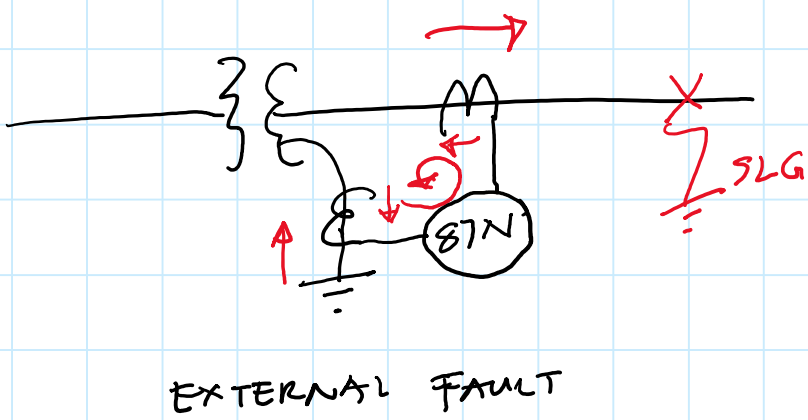
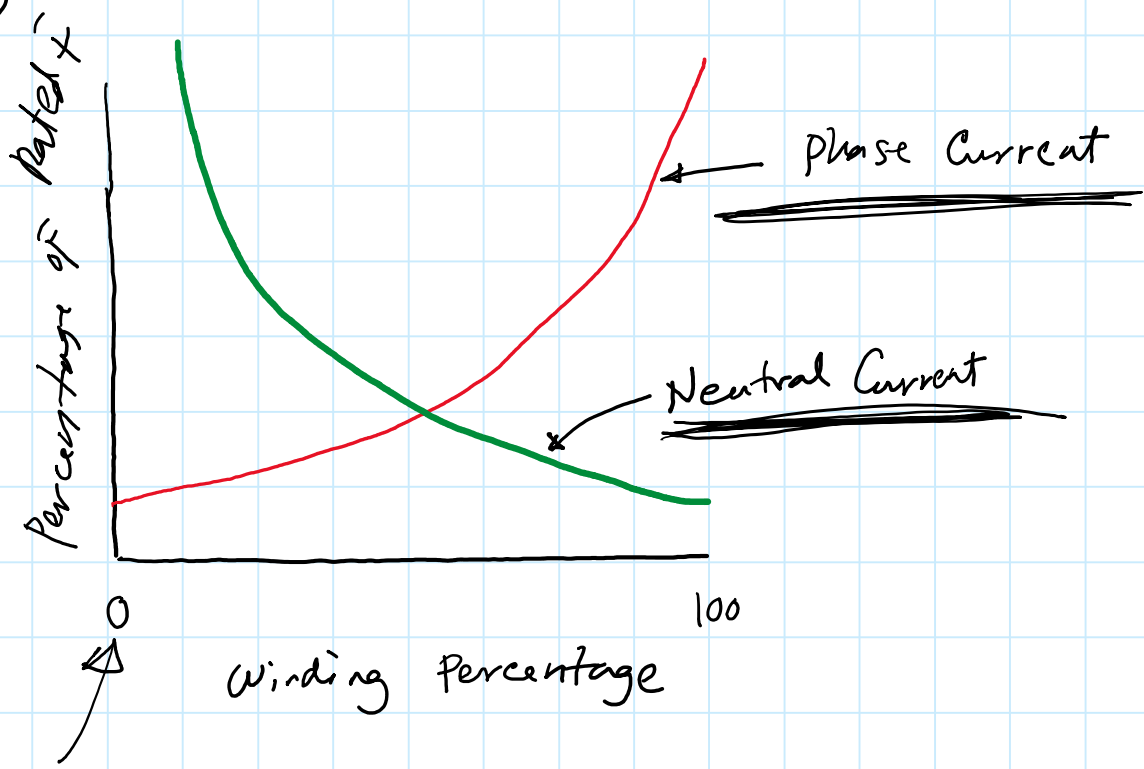
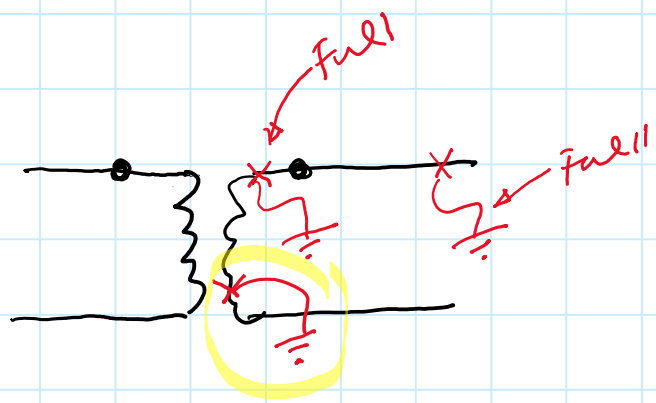
$$OV(59) P_u = 115\% \times V_{PRI} / PTR$$



Say 8 feeders, then SIG P.U = 8X

10% - 40% × I<sub>FL</sub> (or SI)

# Restricted Earth Fault (87N or 64REF)



$$T = \text{Re} [I_x \cdot I_y^*]$$

Taking  $I_y$  as reference:  $I_y = |I| \angle 0^\circ$

For External Fault:

$$I_y = |I| \angle 0^\circ ; I_x = |I| \angle 180^\circ$$

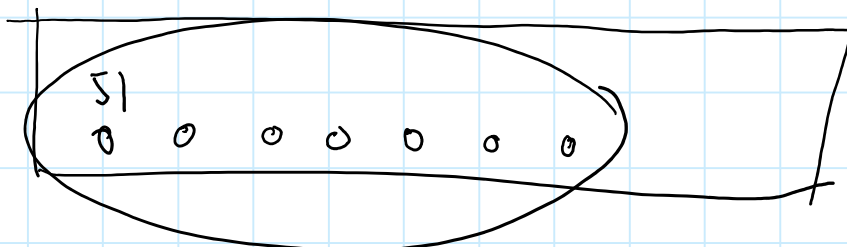
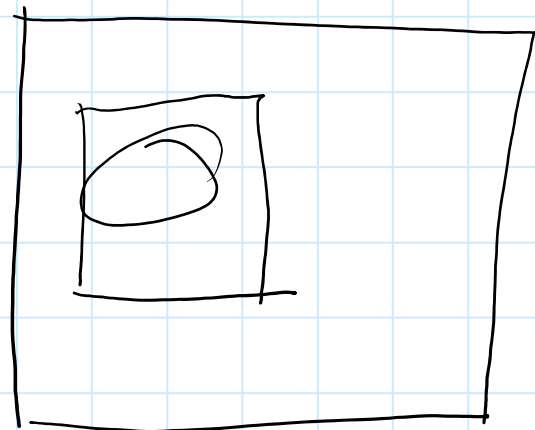
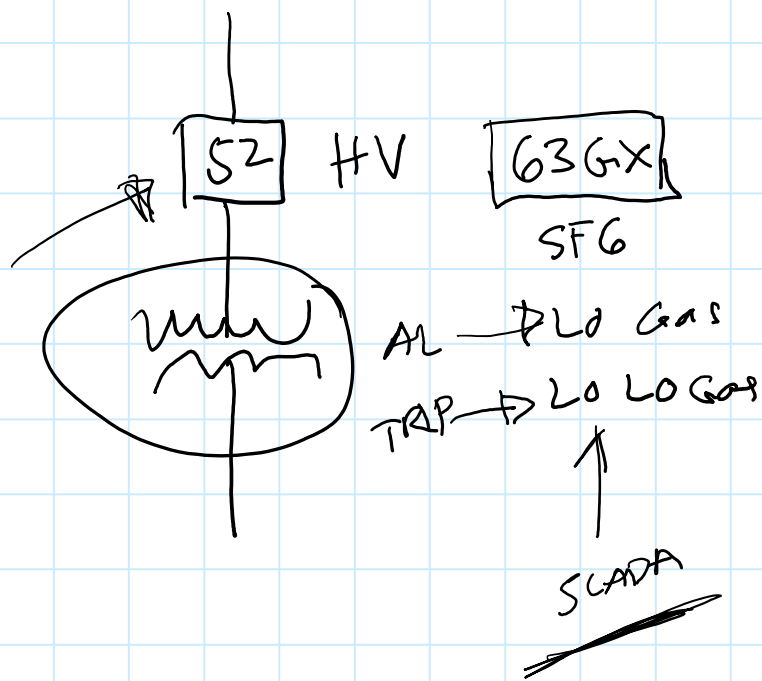
$$T = \text{Re} [ |I| \angle 180^\circ \cdot |I| \angle 0^\circ ] \text{ (yields negative for Real part)}$$

For Internal Fault:

$$I_y = |I| \angle 0^\circ ; I_x = |I| \angle 0^\circ$$

$$T = \text{Re} [ |I| \angle 0^\circ \cdot |I| \angle 0^\circ ] \text{ (yields positive for real part)}$$

$$\text{Re} = |I| \cdot |I| \cos (\theta_x^\circ - \theta_y^\circ)$$



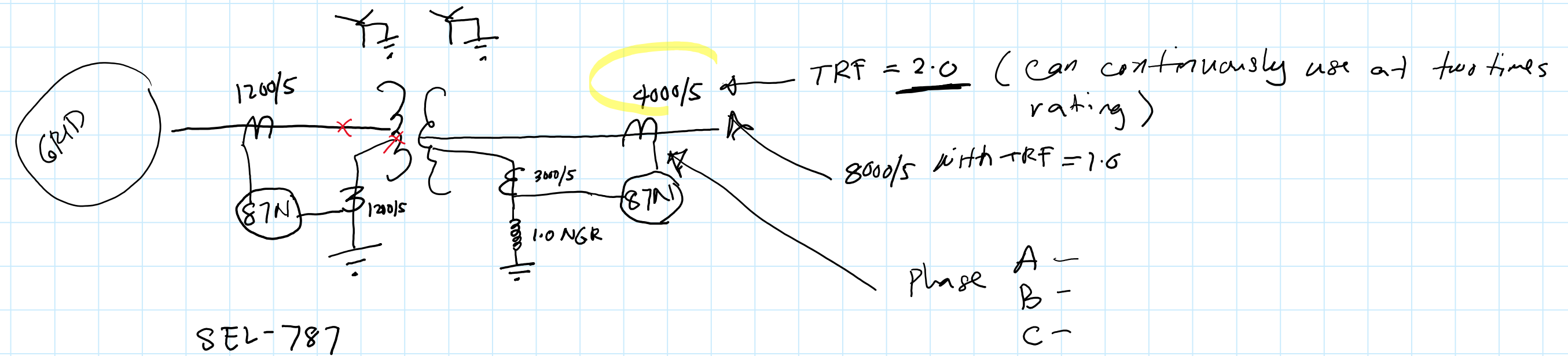
Example for 87N Setting:

Transformer Data : 240 MVA , 245 KV , 34.5 KV , 3  $\phi$

$$I_{PRI} = 401.6 \text{ AMP}$$

$$I_{SEC} = 4016.3 \text{ AMP}$$

$$125\% \times FLA$$



- CRITERIA:
- ① Must be greater than natural residual unbalance by load condition
  - ② Must be greater than minimum value determined by the relationship of the  $CTR_n$  values used in the REF function

CRITERIA #1 Evaluation:

MV SIDE (34.5 KV)

$$I_{MAXH} = 401.6 \text{ A}$$

$$4016.3$$

$$I_{REFH} = 10\% \times I_{MAXH} = 40.16 \text{ A}$$

$$401.6$$

Secondary Amps:

$$I_{REFH}(\text{sec}) = 40.16 / CTR_H = 40.16 / (1200/5) = 0.167 \text{ A}$$

$$\text{Per Unit : } I_{REFH}(\text{sec}) / \text{Relay Rating} = 0.167/5 = \underline{0.033 \text{ P.U.}}$$

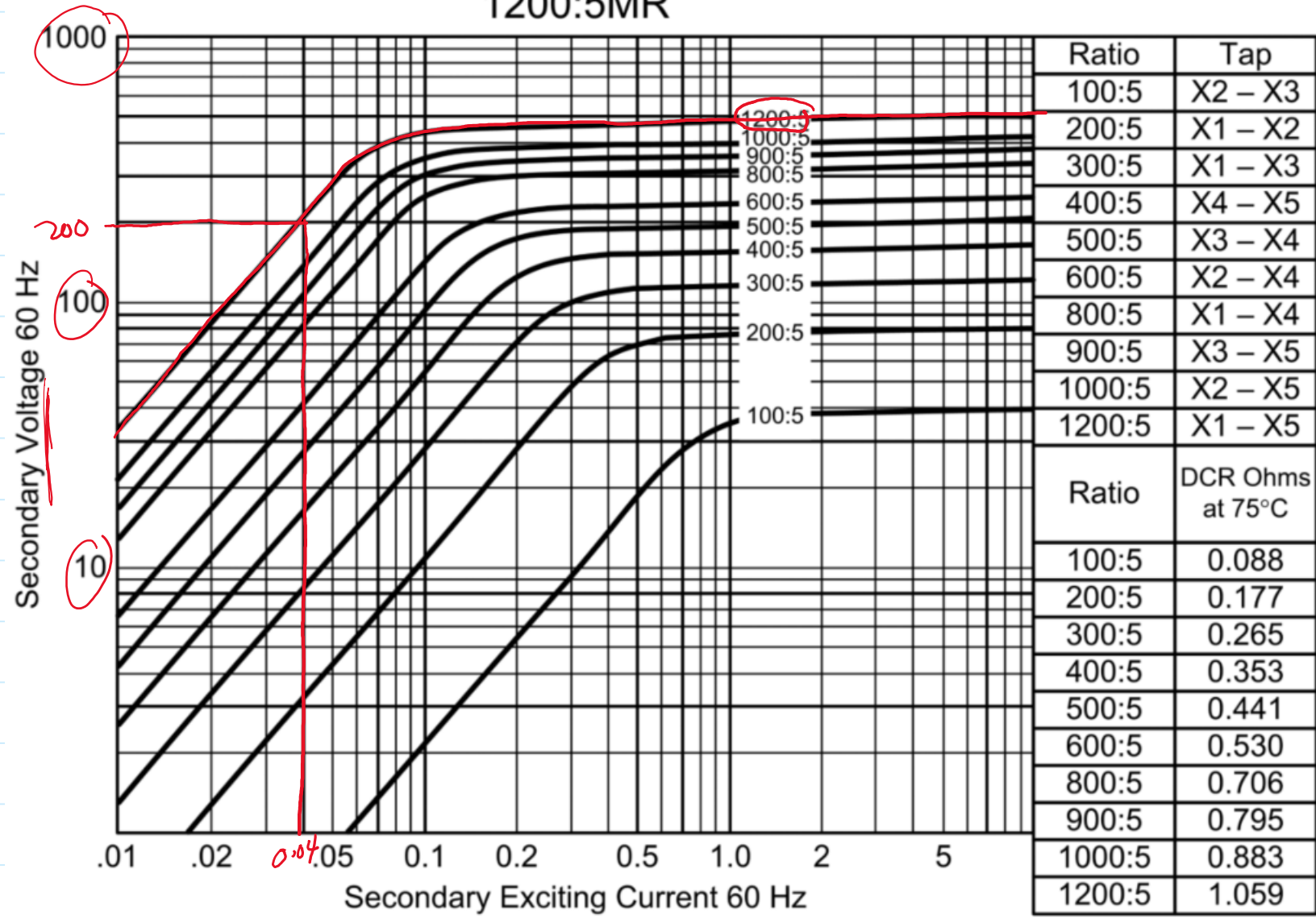
CRITERIA #2 Evaluation (Compare the relative sensitivity of winding CT to Neutral CT):

$$I_{REF} = 0.05 \frac{CTR_H \cdot 5A}{CTR_{HS.N} \cdot 5A} = \frac{0.05 (1200/5) \cdot 5}{(1200/5) \cdot 5} = \underline{0.05 \text{ pu}}$$

Choose : 0.10 pu setting for H.S. REF protection

$$\text{Primary Amp : } 0.1 \text{ pu} \times 5 = 0.5 \text{ AMP} \rightarrow 0.5 \times \frac{1200}{5} = 120 \text{ AMP (Primary)}$$

# 1200:5MR

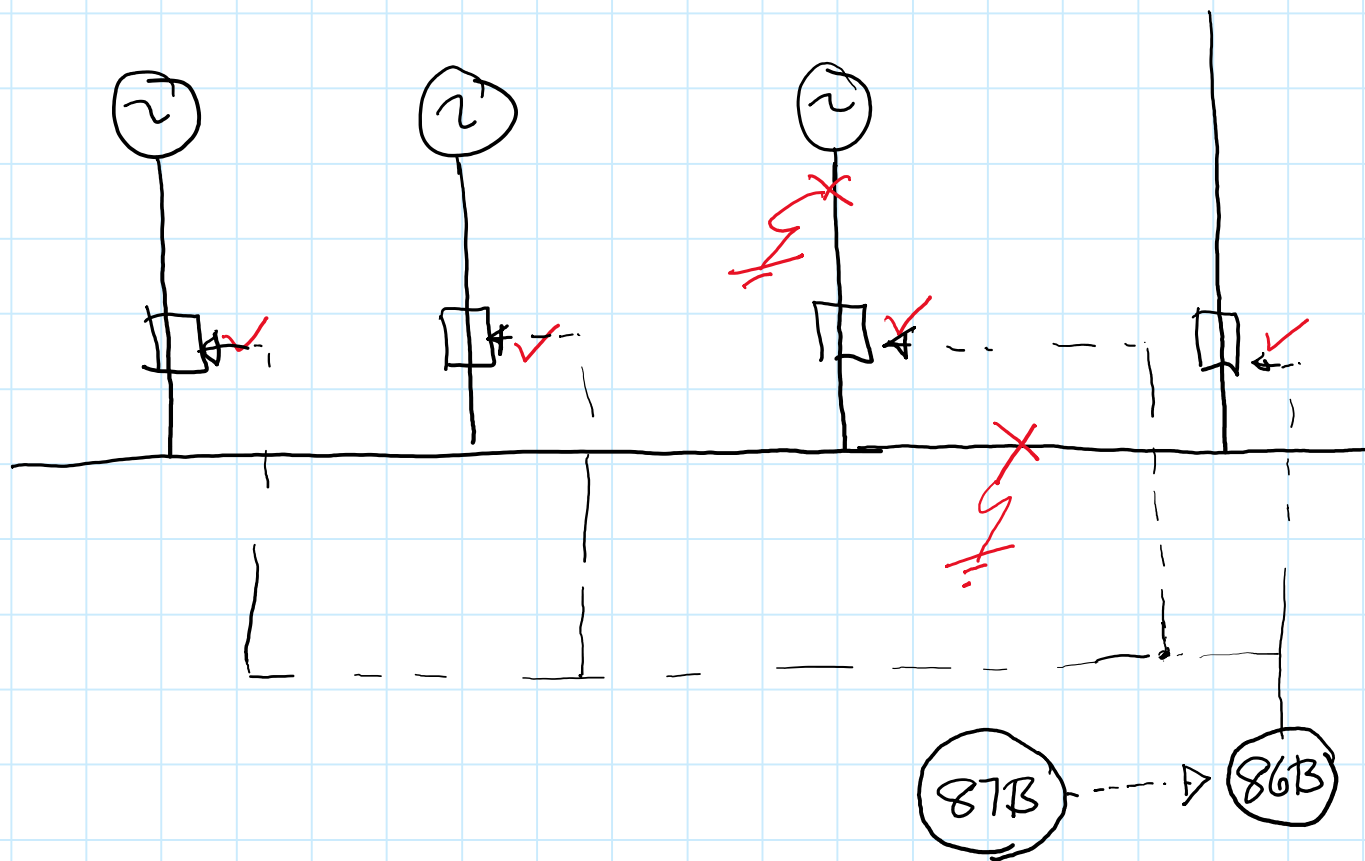


Ratio	Tap
100:5	X2 - X3
200:5	X1 - X2
300:5	X1 - X3
400:5	X4 - X5
500:5	X3 - X4
600:5	X2 - X4
800:5	X1 - X4
900:5	X3 - X5
1000:5	X2 - X5
1200:5	X1 - X5

Ratio	DCR Ohms at 75°C
100:5	0.088
200:5	0.177
300:5	0.265
400:5	0.353
500:5	0.441
600:5	0.530
800:5	0.706
900:5	0.795
1000:5	0.883
1200:5	1.059





NOTE: Select CTs with the same  
 (1) Ratio (2) Voltage class  
 (3) Same manufacturer

$$\frac{4000}{5} \text{ tap } 2 \frac{3000}{5}$$

$$R_L = 0.5 \Omega$$

$$R_{CT} = 0.025 \Omega$$

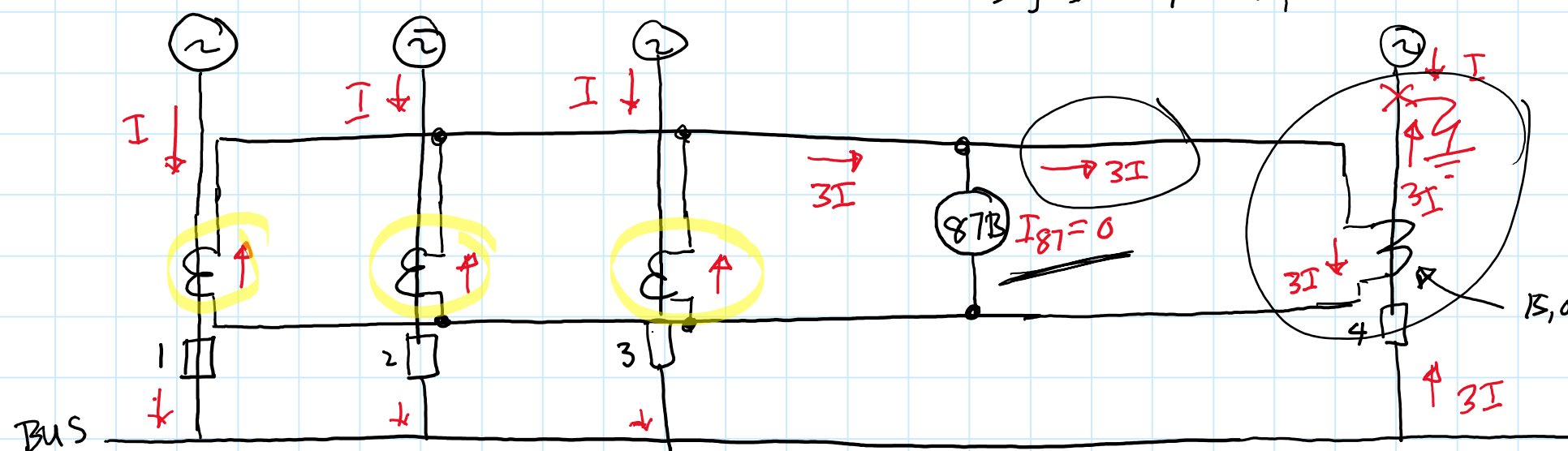
$$R_R = 0.5 \Omega$$

$$CTR = 600/5$$

$$R = 10 \Omega$$

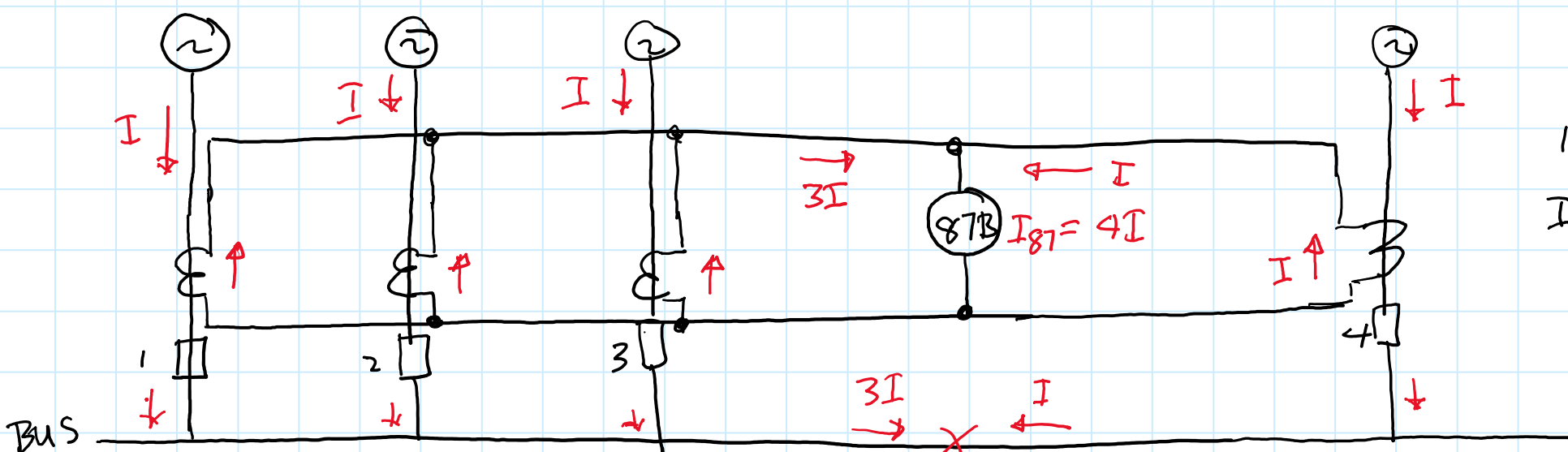
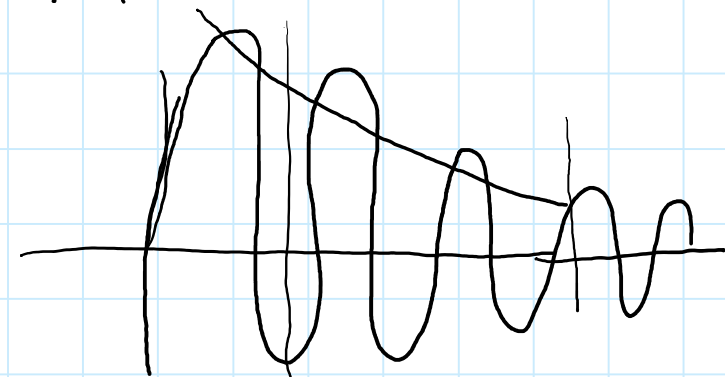
### DIFFERENTIAL OVERCURRENT PROTECTION

Say  $I = 5,000$  Amps



$$\left(1 + \frac{X}{R}\right) I_F = Z_b$$

EXTERNAL FAULT  
 15,000 AMPS (Ctn Saturate)

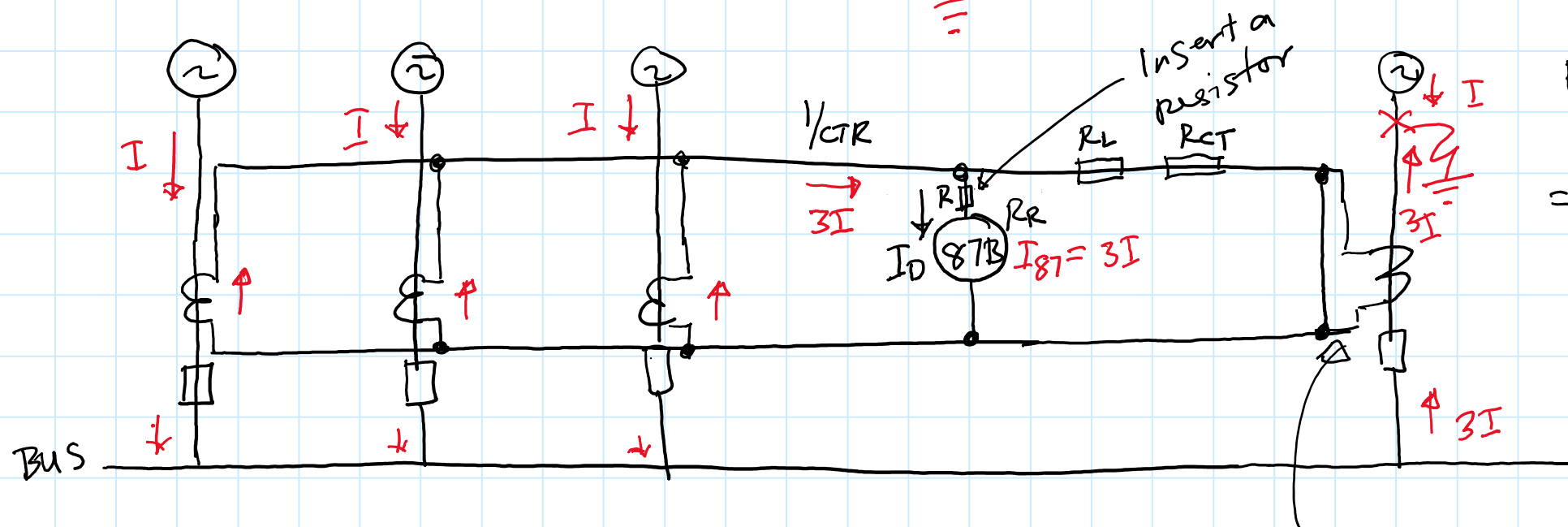


INTERNAL FAULT

$$I_D = \frac{0.5 + 0.025}{0.5 + 0.25 + 0.5} \cdot \frac{20,000}{600/5}$$

$$= 85.37 \text{ AMPS}$$

$$= 8.33 \text{ AMPS (with } R)$$



External Fault with Saturated CT

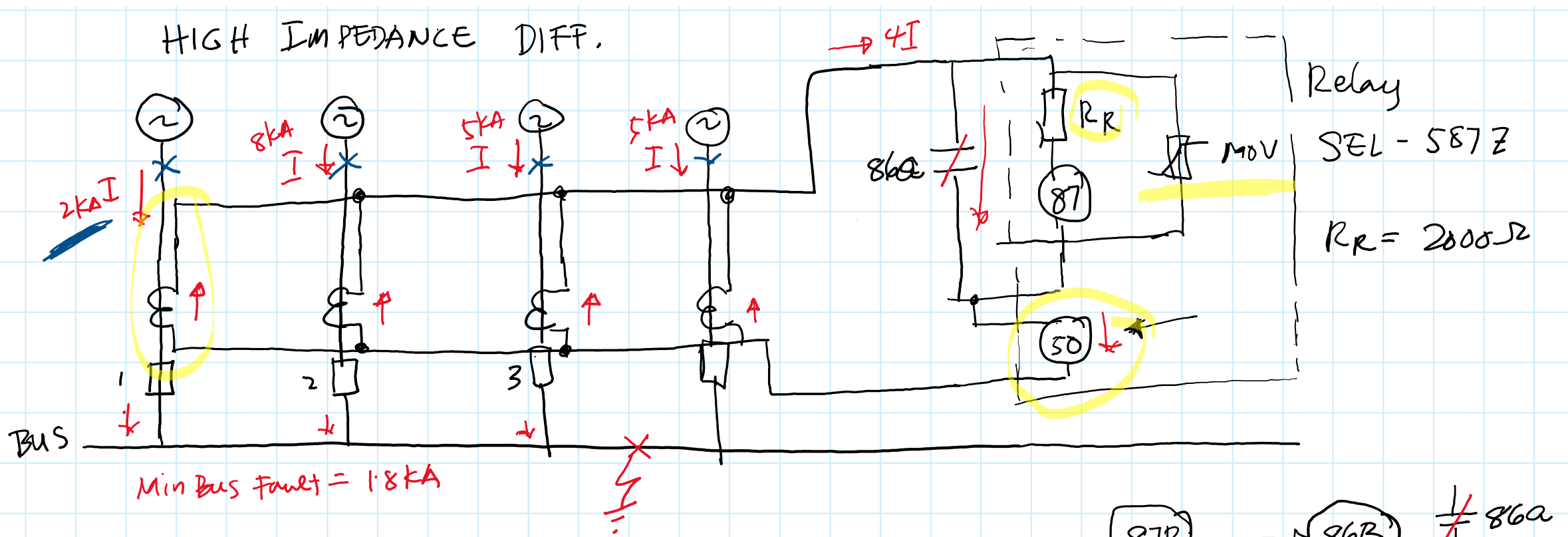
$$I_D = \frac{R_L + R_{CT}}{R_L + R_{CT} + R_R} \cdot \frac{I}{CTR}$$

$$I_D = \frac{0.5 + 0.025}{0.5 + 0.25 + 0.5} \cdot \frac{15000}{600/5}$$

$$= 64.02 \text{ AMPS}$$

$$= 5.95 \text{ AMPS (with } R)$$

# HIGH IMPEDANCE DIFF.



$$V_{pu} = K_s \cdot (n \cdot R_L + R_{CT}) \cdot I / CTR$$

$K_s$  = safety factor (typically 1.5 to 2)

$R_L$  = lead/conductor resistance

$R_{CT}$  = CT secondary resistance

$n$  = use 1 for 3φ or 2 for single-phase

$$I_{min} = (N \cdot I_E + I_{relay} + I_{MOV}) \cdot CTR$$

$N$  = # of CTs

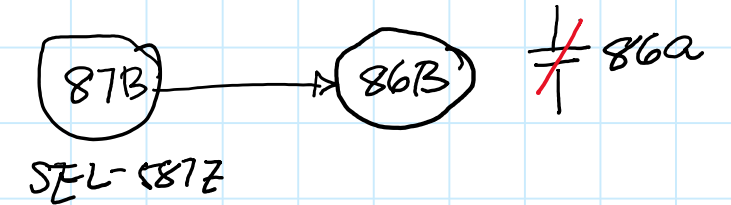
$I_E$  = excitation current

$I_{relay}$  = relay current

$$V_{pu} = K_D \cdot V_{STD}$$

$V_{STD}$  = accuracy class of CT

$K_D$  = security factor (0.5 to 1)



Fault Data :	3 $\phi$	SLG
F1	2kA	1.2kA
F2	8kA	8.8kA
F3	5kA	3.5kA
F4	5kA	3.5kA
Min Bus	1.8kA	<u>0.9kA</u>

CT circuits Data

$$R_L = 0.4 \Omega$$

$$R_R \text{ (stabilizing Relay Resistor)} = 2000 \Omega$$

$$R_{CT} = 1.06 \Omega$$

$$CTR = 1200/5$$

$$CT \text{ accuracy class} = C400$$

④ Calculate OC element pickup setting

$$I_{pu} = K_1 \cdot \frac{I_{MIN}}{CTR} = 0.5 \frac{900}{1200/5}$$

$$I_{pu} = 1.875 \text{ A}$$

① Calculate for Short Circuit Currents

$$I_{3\phi\_INT} = 2 + 8 + 5 + 5 = 20 \text{ kA}$$

$$I_{SLG\_INT} = 1.2 + 8.8 + 3.5 + 3.5 = 17 \text{ kA}$$

} Max Internal Fault

$$I_{3\phi\_EXT} = 8 + 5 + 5 = 18 \text{ kA}$$

$$I_{SLG\_EXT} = 8.8 + 3.5 + 3.5 = 15.8 \text{ kA}$$

} Max External Fault

$$I_{3\phi\_MIN} = 18 \text{ kA}$$

$$I_{SLG\_MIN} = 0.9 \text{ kA}$$

} Minimum Internal Faults

② Calculate secure voltage setting

$$V_{pu} = K_S \cdot (N \cdot R_L + R_{CT}) \cdot I / CTR = 1.5 (1 \times 0.4 + 1.06) \cdot 16,000 / (1200/5) = 164.25 \text{ V (3}\phi)$$

$$V_{pu} = K_S \cdot (N \cdot R_L + R_{CT}) \cdot I / CTR = 1.5 (2 \times 0.4 + 1.06) \cdot 15,800 / (1200/5) = 183.68 \text{ V (1}\phi)$$

② Calculate dependable voltage setting

$$V_{pu} = K_D \cdot V_{STD} = 0.5 \times 400 = 200 \text{ V}$$

③ Calculate sensitivity for Internal Faults

$$I_{MIN} = (N \cdot I_E + I_{RELAY} + I_{MOV}) \cdot CTR = (4 \times 0.04 + \frac{200}{2000} + 0) \cdot \frac{1200}{5} = 62.4 \text{ Amp primary}$$

Since  $62.4 < 900$  then sensitivity is satisfied

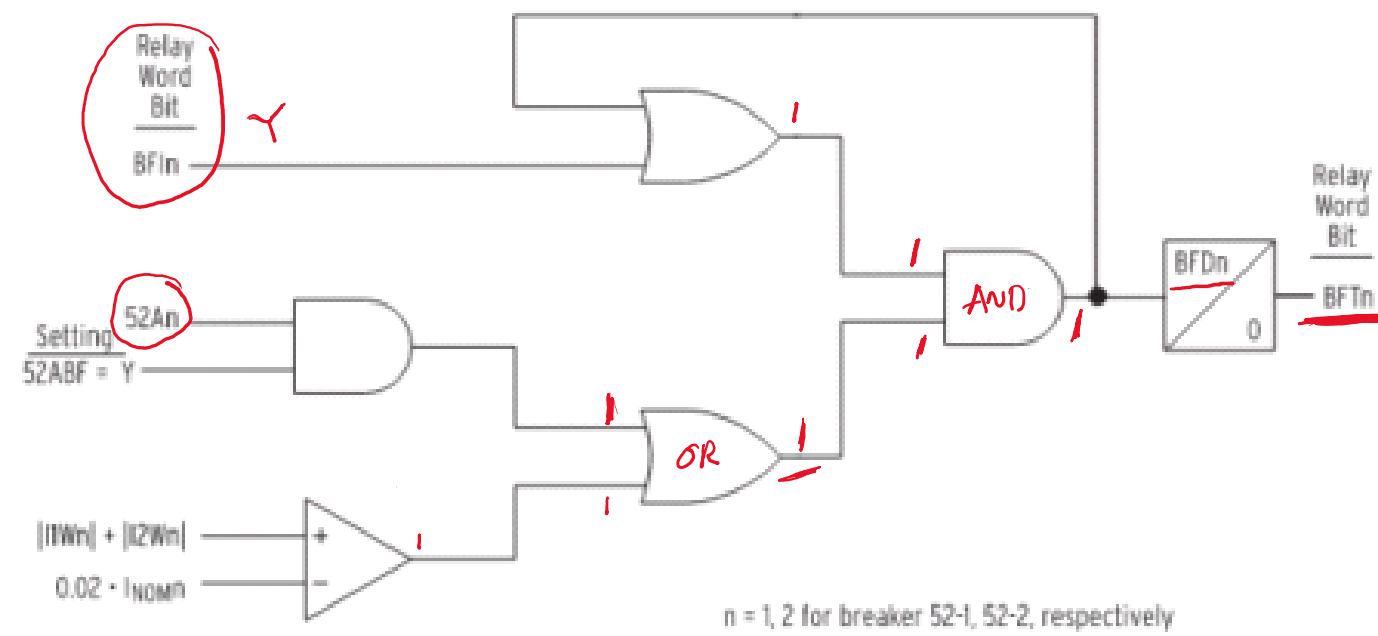
# Breaker Failure Setting

**Table 4.38 Breaker Failure Setting**

Setting Prompt	Setting Range	Setting Name := Factory Default
52A INTERLOCK	Y, N	52ABF := N
BRKR1 FAIL DELAY	0.00–2.00 sec	BFD1 := 0.50
BRKR1 FAIL INIT	SELOGIC	BF11 := R_TRIG TRIP1 OR R_TRIG TRIPXFMR
BRKR2 FAIL DELAY	0.00-2.00 sec	BFD2 := 0.50
BRKR2 FAIL INIT	SELOGIC	BF12 := R_TRIG TRIP2 OR R_TRIG TRIPXFMR

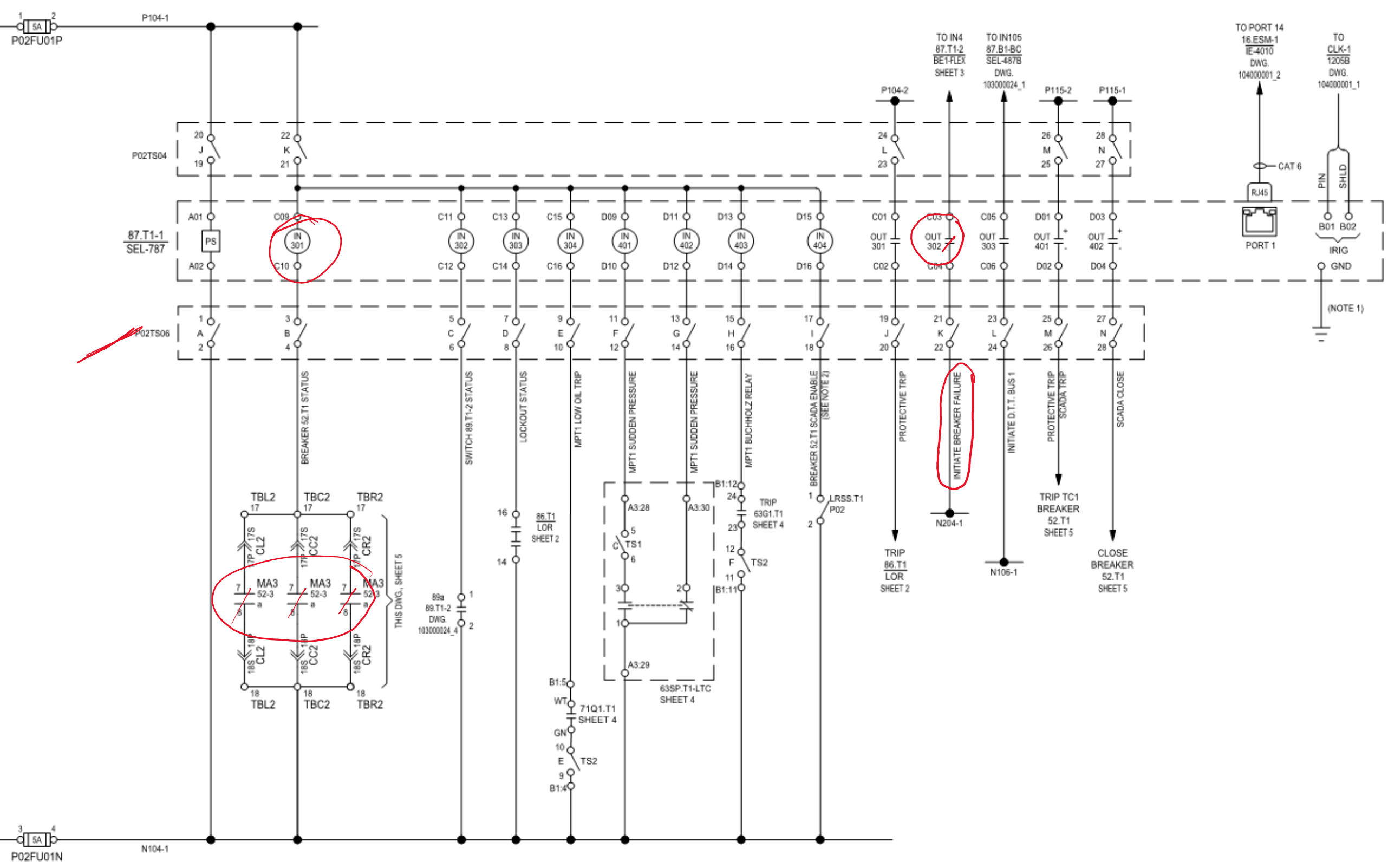
The SEL-787 provides flexible breaker failure logic (see *Figure 4.57*) for two breakers. In the default breaker failure logic, assertion of trip Relay Word bits associated with a breaker starts a BFD timer if the sum of positive and negative-sequence breaker current is above  $0.02 \cdot I_{NOM}$ . If the current remains above the threshold for BFD delay setting, Relay Word bit BFT will assert. Use the BFT to operate an output relay to trip appropriate backup breakers. Changing the BFI and/or 52ABF settings can modify the default breaker failure logic.

- Set BF11 = R\_TRIG TRIP1 OR R\_TRIG TRIPXFMR AND NOT IN102 if input IN102 is manual trip only and breaker failure initiation is not desired when the tripping is caused by this input.
- Set 52ABF = Y if you want the breaker failure logic to detect failure of breaker/contact auxiliary contact to operate during the trip operation as defined by the BFI setting.

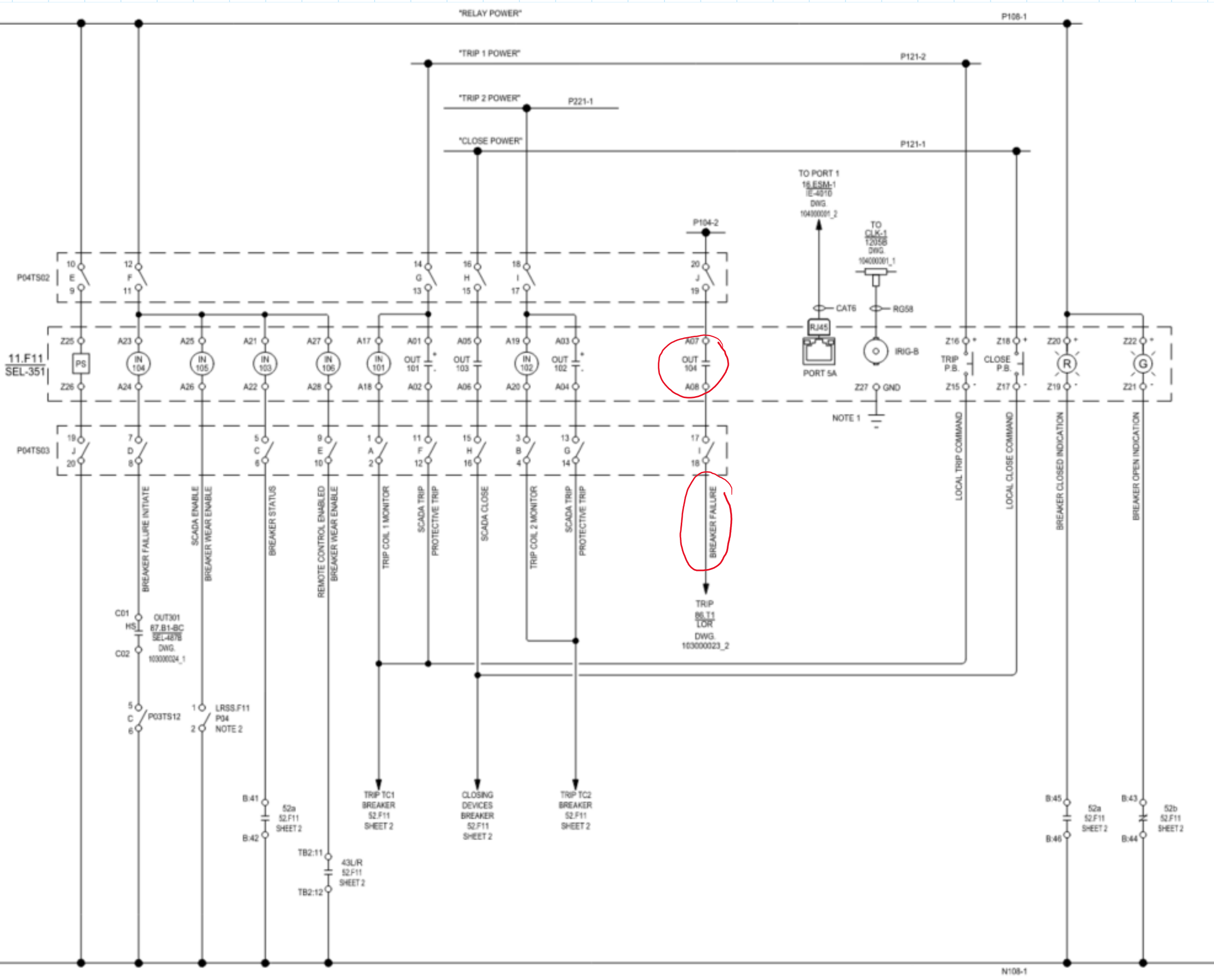


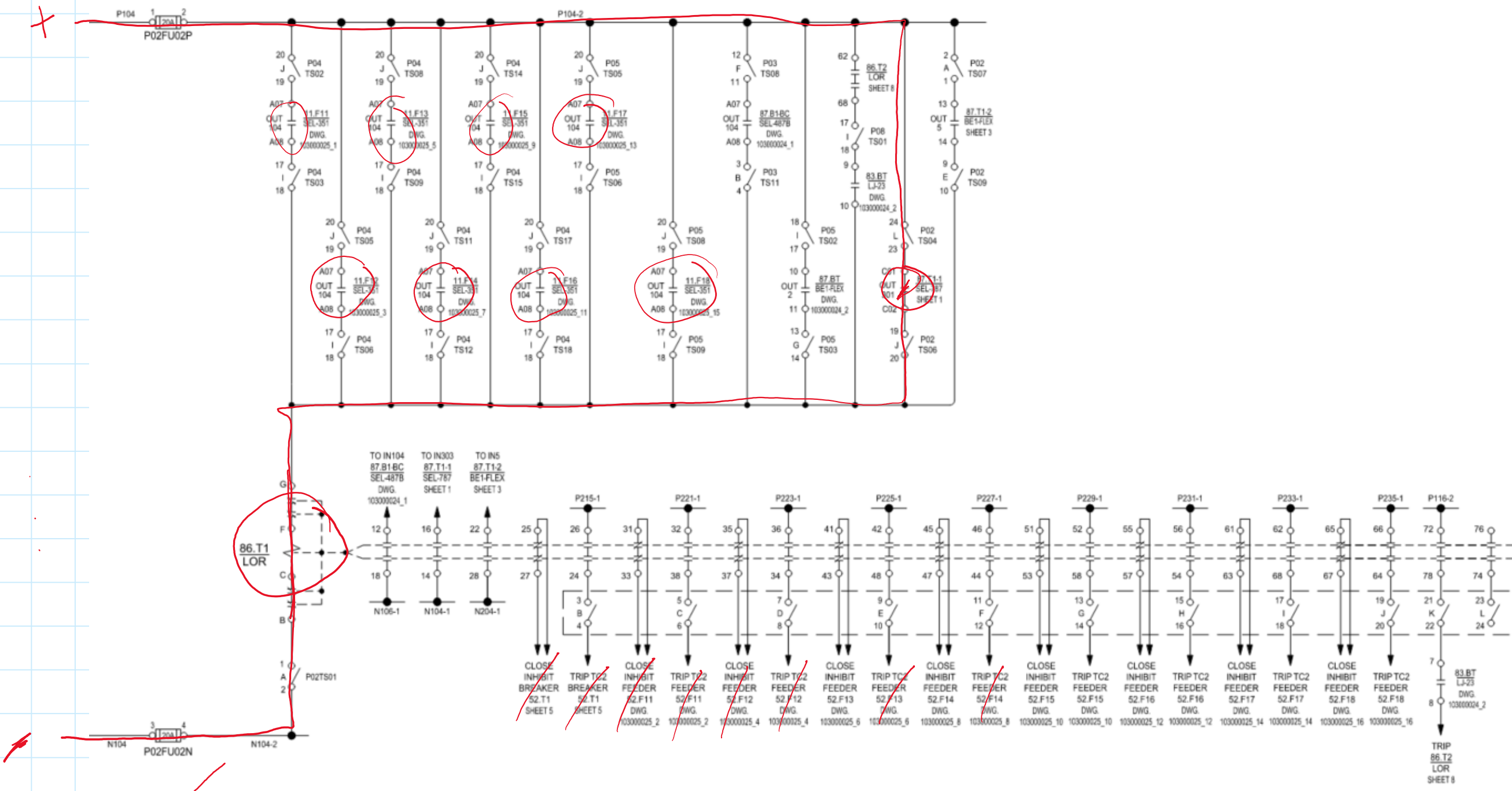
**Figure 4.57 Breaker Failure Logic**

Handwritten notes in red ink:  $0.02 \cdot I_{nom}$ ,  $I1W1$  positive,  $I2Wn$  neg, 52a - Breaker Aux Contact

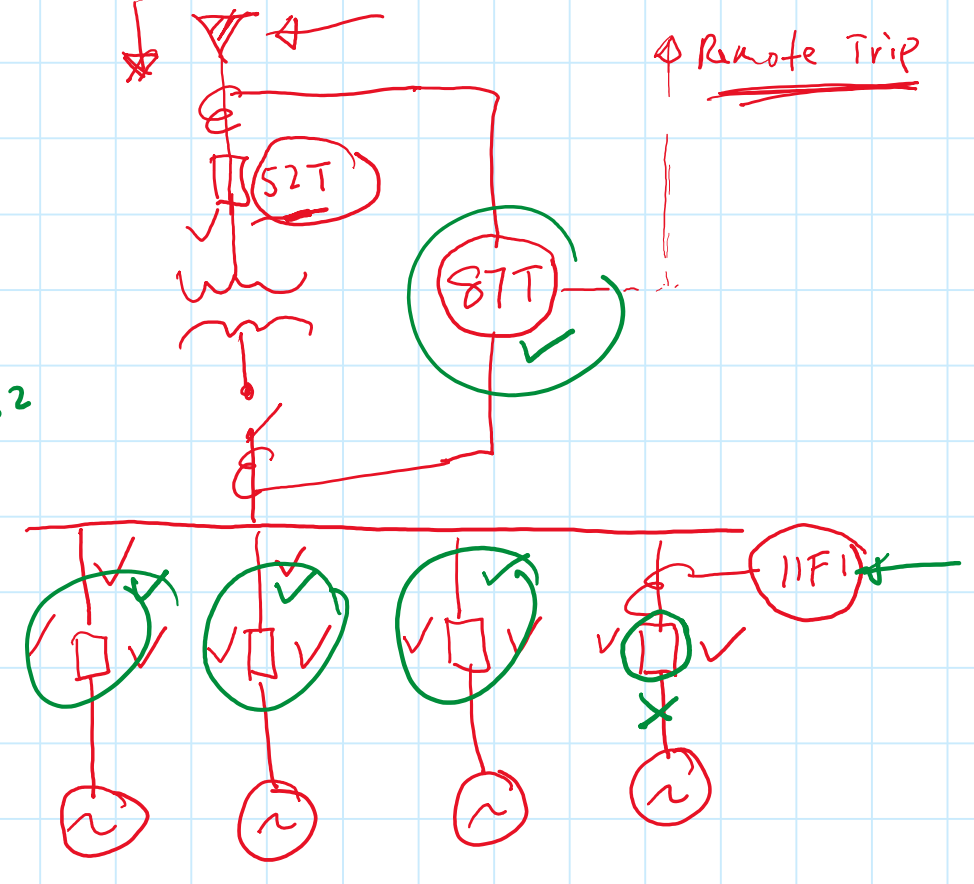








86B2 → Trip all breakers at Bus 2  
 87BT-a  
 86B1 → all breakers at Bus 1



IEC 61850

